Math 225:	Calculus III	Name:
Exam III	Apr. 14, 1994	Section:

Record your answers to the multiple choice problems by placing an \times through one letter for each problem on this answer sheet. There are 15 multiple choice questions worth 6 points each. You start with 10 points. Find the area of the region enclosed by the curve $r = \sqrt{3 - 2\sin(2\theta)}$.

 $3\pi \ 2\pi \ 5\pi/3 \ 7\pi/3\pi \ 8\pi/3$

Evaluate $\int_0^1 \int_0^{\sqrt{x}} \int_0^y e^{-x^2} dz \, dy \, dx \ (1-e^{-1})/4 \ 1/4 \ e^{-1}/2 \ (e-1)/2 \ (e^{-1}-1)/2$ Find the volume of the solid region in the first octant bounded by the plane x + y = 1 and the surface $z = \sin(\pi x)$. $1/\pi \pi 1/2 \pi/2 1$

Let *R* be the region defined by $1 \le x \le 2$, $1 \le xy \le 2$. Using the substitution u = x, v = xy, transform $_{R}y \, dA$ into an iterated integral in the *uv*-plane. $\int_{1}^{2} \int_{1}^{2} \frac{v}{u^{2}} \, du \, dv \int_{1}^{2} \int_{1}^{2/u} \frac{v}{u} \, du \, dv \int_{1}^{2} \int_{1}^{2v/u} \frac{1}{u^{2}} \, du \, dv \int_{1}^{2} \int_{1}^{2} \frac{v}{u} \, du \, dv \int_{1}^{2} \int_{1}^{2v/u} \frac{1}{u^{2}} \, du \, dv$

Let D be the solid region below the paraboloid $z = 4 - x^2 - y^2$ and above the xy-plane. The density of D is given by $\delta(x, y, z) = 4 - z$. Given that the total mass of D is $64\pi/3$, compute the center of mass of D. (0,0,1) (0,0,7/8) (0,0,3/4) (0,0,5/4) (0,0,3/2)

Find the volume of the solid region between the cone $z^2 = 4(x^2 + y^2)$ and the paraboloid $z = 1 + x^2 + y^2$.

 $\pi/6 \pi 3\pi/4 \pi/2 \pi/3$

Find the average value of $f(x, y, z) = (x^2 + y^2 + z^2)^{1/2}$ over the solid unit ball, $x^2 + y^2 + z^2 \le 1$. 3/41/2 5/8 7/8 2/3

Find the vector field represented in the following plot:

$$\begin{array}{l} \frac{1}{2\sqrt{x^2+1}} \subset +\frac{x}{2\sqrt{x^2+1}} \supset \frac{x}{2\sqrt{x^2+y^4}} \subset +\frac{y^2}{2\sqrt{x^2+y^4}} \supset \frac{x}{2\sqrt{x^2+1}} \subset -\frac{x^2}{2\sqrt{x^4+1}} \supset -\frac{y}{10} \subset +\frac{x}{10} \supset \frac{x}{10} \subset +\frac{y}{10} \supset \frac{x}{10} \supset \frac{x}{10} \subset +\frac{y}{10} \supset \frac{x}{10} \supset \frac{x}{10$$

 $0 \le t \le 1$. Compute the flow integral $\int_{\mathcal{C}} d$. -9/5 - 7/3 - 7/2 - 9/4 - 11/6Let \mathcal{C} be a smooth curve from (1, 1, 0) to (0, 0, 1). Compute

$$\int_{\mathcal{C}} -yz\sin(xz)\,dx + \cos(xz)\,dy - xy\sin(xz)\,dz$$

 $-1 - 3\cos(1)\cos(1) 2 0$

Let C be the boundary of the region inside the unit circle in the first quadrant (oriented counterclockwise). Use Green's Theorem to evaluate $\int_{C} x^2 y \, dx - xy^2 \, dy$.

 $-\pi/8 \pi - \pi/3 \pi/4 - 3\pi/4$

Determine which of the following formulas is true for an arbitrary function f or vector field . $\div = 0$ $\div f = 0 = \div = \div =$