

Record your answers to the multiple choice problems by placing an \times through one letter for each problem on this answer sheet. There are 15 multiple choice questions worth 5 points each. You start with 25 points.

Find parametric equations of the line perpendicular to the surface defined by $x^2y - z^2 = 1$ at the point $(1, 2, 1)$.
 $x = 1 + 4t, y = 2 + t, z = 1 - 2t$
 $x = 1 + 2xyt, y = 2 + x^2t, z = 1 - 2zt$
 $x = 1 + t, y = 2 + 2t, z = 1 - t$
 $x = t, y = 2t, z = -t$
 $x = 1 - 4t, y = 2 + t, z = 1 + t$

Determine which function below has a graph like the following:

$f(x, y) = y^3 - y^2 - x^2$
 $f(x, y) = y - x - 1$
 $f(x, y) = y^2 - y - x$
 $f(x, y) = x - y^2 + y$
 $f(x, y) = x^2 - y^3 + y$

Compute the slope of the line tangent to the plane curve defined by the equation $x^2y^3 - x + y^2 = 1$ at the point $(1, 1)$.
 $-1/5$ $1/4$ 6 1 $-1/6$

If $f(x, y, z) = \cos(x^2y)e^{-z} + e^{y^2}x^3$, compute $f_{xz}(1, \pi/2, 0)$.

π 0 1 2 $-\pi/e$

Suppose $f(x, y)$ satisfies $f_x(6, 13) = -4$ and $f_y(6, 13) = 3/2$. If $x = uv$, and $y = u^2 + v^2$, compute $\frac{\partial f}{\partial v}$ at the point $(u, v) = (3, 2)$.

-6 5 -9 1 8

Find the derivative of $f(x, y, z) = y \log(x + 3) - 2xz^2e^y$ at the point $(-2, 0, 3)$ in the direction of the vector $-\mathbf{i} - 2\mathbf{j} + 2\mathbf{k}$.

-2 -6 $(18, 36, 24)$ $(-18, -72, 48)$ -3

Compute the gradient of the function $f(x, y, z) = \sin(xy) + y^3 - xz^2$ at the point $(\pi, 1, 2)$.

-5 $\mathbf{i} + (3 - \pi)\mathbf{j} - 4\pi\mathbf{k}$
 $-\mathbf{i} + 3\mathbf{j} - 4\pi\mathbf{k}$
 $-(1 + 4\pi)\mathbf{i} + 2\mathbf{j} - 4\mathbf{k}$
 $-\mathbf{i} + 3\mathbf{j} - (2 - \pi)\mathbf{k}$
 -5 $\mathbf{i} - \pi\mathbf{j} - 4\mathbf{k}$

Determine the equation of the plane tangent to the graph of $f(x, y) = x^3 - 3x^2y + 2y^4$ at the point $(1, 1, 0)$.

$$3x - 5y + z = -2 \quad 3x - y + z = 2 \quad 6x - 8y + z = 2 \quad 6x - 4y - z = 2 \quad 3x - 5y = -2$$

Find all the critical points of the function $f(x, y) = 5x^3 - 21xy^2 + 14y^3 + 24x + 3$.

$(-2, -2), (2, 2) (1.36, 0), (-1.36, 0), (-2, -2), (2, 2) (-2, -2), (-2, 2), (2, -2), (2, 2), (1.36, 0), (-1.36, 0), (-2, 2), (2, -2) (1.36, 0), (-1.36, 0)$

Choose the statement below that is **true** about the function $f(x, y) = e^{-y}(x^2 + y^2)$.

$(0, 2)$ is **not** a critical point of f f has a local minimum at $(0, 2)$ f has a local maximum at $(0, 2)$ f has a saddle point at $(0, 2)$ none of the above

Find the minimum of $f(x, y) = x^3 - 6xy + y^2$ on the rectangle $0 \leq x \leq 10, 0 \leq y \leq 20$.
 $-108 \quad -106 \quad -120 \quad -200 \quad 0$

Find a point on the curve $13x^2 + 10xy + 13y^2 = 4$ where the value of the function $f(x, y) = x^2y^2$ is greater than or equal to its value at any other point on the curve.

$(\frac{1}{2}, -\frac{1}{2}) (\frac{1}{3}, \frac{1}{3}) (-1, 1) (1, -\frac{1}{\sqrt{5}}) (\frac{2}{\sqrt{13}}, -\frac{2}{\sqrt{13}})$

Compute $\int_0^1 \int_0^y e^{y^2} dx dy$. $(e - 1)/2 \quad e \quad 0 \quad \frac{1}{2} - e \quad 1$

Reverse the order of integration in the integral $\int_1^2 \int_1^{y^3} f(x, y) dx dy \int_1^8 \int_{x^{1/3}}^2 f(x, y) dy dx$
 $\int_1^{y^3} \int_1^2 f(x, y) dy dx \int_1^2 \int_{y^3}^1 f(x, y) dy dx \int_0^8 \int_{x^3}^2 f(x, y) dy dx \int_0^8 \int_0^{x^{1/3}} f(x, y) dy dx$

The area of the region bounded by $y = 9 - x^2$ and the x -axis is 36. Find the centroid of this region.

$(0, 3.6) (0, 4.0) (0, 2.4) (0, 3.2) (0, 2.8)$