

Record your answers to the multiple choice problems by placing an \times through one letter for each problem on this page. There are 20 multiple choice questions worth 6 points. You start with 30 points.

You may use a calculator if you wish.

Find the arc length of the curve described by the vector function $\mathbf{r}(t) = 2 \cos(\pi t^2)\mathbf{i} + \sqrt{2} \sin(\pi t^2)\mathbf{j} - \sqrt{2} \sin(\pi t^2)\mathbf{k}$ for $0 \leq t \leq 1$.

$2\pi \quad 4\pi \quad 2 \quad 4 \quad 16\pi^2/3$

Let $\mathbf{v} = \langle t, t^2, t^3 \rangle$ for a real number t , and let $\mathbf{w} = \langle 1, 1, 1 \rangle$. Find the vector projection $\text{proj}_{\mathbf{w}}(\mathbf{v})$ of \mathbf{v} on \mathbf{w} .

$\frac{t+t^2+t^3}{3} \langle 1, 1, 1 \rangle \quad \frac{t^2+t^4+t^6}{3} \quad \frac{t+t^2+t^3}{\sqrt{3}} \quad (t+t^2+t^3) \langle 1, 1, 1 \rangle \quad \frac{t+t^2+t^3}{\sqrt{3}} \langle t, t^2, t^3 \rangle$

Suppose that the acceleration of an object at time $t \geq 0$ is given by $\mathbf{a}(t) = 2t\mathbf{i} + 2\mathbf{k}$, that the object's position at time $t = 0$ is $\mathbf{r}(0) = \mathbf{i} + \mathbf{j}$, and that its position at time $t = 1$ is $\mathbf{r}(1) = \mathbf{0}$. Find $\mathbf{v}(0)$, the object's velocity at time $t = 0$.

$-4/3\mathbf{i} - \mathbf{j} - \mathbf{k} \quad 0 \quad -2\mathbf{i} - \mathbf{j} - \mathbf{k} \quad t^2\mathbf{i} + 2t\mathbf{k} \quad \mathbf{i} + 2\mathbf{k}$

Determine which of the following represents the area of the parallelogram consisting of the points

$(u + 1, 2u + 3v + 1, -u + v + 1), \quad 0 \leq u \leq 1, \quad 0 \leq v \leq 1$

$\frac{|(\mathbf{i}+2\mathbf{j}-\mathbf{k}) \times (\mathbf{3j}+\mathbf{k})| \cdot |(\mathbf{i}+5\mathbf{j}) \times (\mathbf{i}+\mathbf{j}+\mathbf{k})| \cdot |(\mathbf{2i}+\mathbf{3j}) \times (\mathbf{i}+\mathbf{4j}+\mathbf{2k})| \cdot |(\mathbf{i}+2\mathbf{j}-\mathbf{k}) \times (\mathbf{i}+\mathbf{4j}+\mathbf{2k})|}{(\mathbf{i} + 2\mathbf{j} - \mathbf{k}) \cdot (\mathbf{3j} + \mathbf{k})}$

Find equations for the line of intersection of the planes $x - y + z = 2$ and $2x + z = 1$.
 $x = -t, y = -1 + t, z = 1 + 2t \quad x = 1/2 - t, y = -3/2 - t, z = t \quad x = t, y = -1 + t, z = 1 - 2t \quad x = 1/2 + t, y = -3/2, z = -t \quad x = 1/2 + t, y = -1 - t, z = -2t$

Compute $\lim_{(x,y) \rightarrow (0,0)} \frac{x^2+y^4}{\sqrt{x^2+y^4+4}-2}$.

$4 \quad 0 \quad 1 \quad -1/2$ does not exist

Let z be the function of x and y defined by equation $xz + e^z y = 2$ Find $\frac{\partial z}{\partial y}$ at the point $(1, 2, 0)$.

$-1/3 \quad -1 \quad 0 \quad 2 \quad -3$

Find the maximum rate of change of the function $f(x, y, z) = x^2 y + e^x z^2$ at point $(0, 1, -1)$.

$$\sqrt{5} \ 1 \ \sqrt{2} \ 0 \ \sqrt{3}$$

Determine which of the following statements describes the function

$$f(x, y) = x^3 - y^3 - 2xy + 6$$

at point $(-2/3, 2/3)$.

f has a local maximum. f has a local minimum. f has a saddle point. The point is not a critical point. The second derivative test is inconclusive.

Find the minimum of $f(x, y, z) = (x-1)^2 + y^2 + z^2$ subject to the constraint $x^2 - yz = 0$.

$$2/3 \ 1/3 \ 1/2 \ 1 \ 2$$

Evaluate $\int_0^1 \int_{e^y}^e \frac{1}{\ln(x)} dx dy$. (Hint: Change the order of integration.)

$$e - 1 \ 1 \ -1 \ e \ 1/\ln(2)$$

Determine which of the following integrals gives the volume of the solid inside the cylinder $x^2 + y^2 = 2x$ above the xy -plane and below the cone $z = \sqrt{x^2 + y^2}$.

$$\int_{-\pi/2}^{\pi/2} \int_0^{2 \cos(\theta)} \int_0^r r dz dr d\theta \quad \int_0^{2\pi} \int_0^2 \int_0^r r dz dr d\theta \quad \int_{-\pi/2}^{\pi/2} \int_0^{2 \cos(\theta)} \int_0^1 z dz dr d\theta \quad \int_{-\pi/2}^{\pi/2} \int_0^2 \int_0^z r dz dr d\theta$$

$$\int_0^\pi \int_0^{2 \cos(\theta)} \int_0^r r dz dr d\theta$$

Evaluate the integral $\int_1^4 \int_0^{1/\sqrt{x}} e^{\sqrt{x}} dy dx$ by using the change of variables $x = u^2$, $y = v$. $2(e^2 - e) \ e - 1 \ 2/e \ 4e^2 - e \ e^{\sqrt{3}} - 1$

Let E be the solid bounded by the cylinder $z = 1 - x^2$ and the plane $y = z$ in the first octant. Determine which of the following integrals equals $\iiint_E f(x, y, z) dV$.

$$\int_0^1 \int_0^{1-x^2} \int_0^z f(x, y, z) dy dz dx \quad \int_0^1 \int_0^{\sqrt{1-z}} \int_0^1 f(x, y, z) dz dx dy \quad \int_0^1 \int_z^1 \int_0^{\sqrt{1-z}} f(x, y, z) dx dy dz$$

$$\int_0^1 \int_0^1 \int_0^{1-x^2} f(x, y, z) dz dx dy \quad \int_0^1 \int_0^{1-x^2} \int_z^1 f(x, y, z) dy dz dx$$

Let E be the solid between the concentric hemispheres $x^2 + y^2 + z^2 = 16$, $z \geq 0$, and $x^2 + y^2 + z^2 = 4$, $z \geq 0$. Assuming the density at each point is inversely proportional to its distance from the origin, find the mass of E . (Let k denote the constant of proportionality.)

$$12k\pi \ 2k\pi \ln(2) \ 48k\pi \ 8k\pi \ 8k\pi^2$$

Let C be the curve $\mathbf{r}(t) = \langle \sin(3t), \sin(t) + 2 \sin(2t), \cos(t) - 2 \cos(2t) \rangle$, $0 \leq t \leq 2\pi$. Compute $\int_C y dx + x dy + z dz$.

$$0 \ 1/2 \ 1 \ 2 \ 3/2$$

Find the equation of the plane tangent to the surface parameterized by

$$\mathbf{r}(u, v) = \langle u - v^2, v - u^2, uv \rangle, \quad -2 \leq u \leq 2, \quad -2 \leq v \leq 2$$

at the point $(0, 0, 1)$.

$$x + y + z = 1 \quad y + z = 1 \quad x - y + z = 0 \quad x + y - z = 0 \quad -x - y + z = 1$$

Suppose the temperature at a point (x, y, z) on the hemisphere $z = \sqrt{1 - x^2 - y^2}$ is $T(x, y, z) = 20z^2$. Determine the average temperature on the hemisphere. The area of the surface is 2π .

$$6.67 \quad 10 \quad 2.09 \quad 15 \quad 12.33$$

Let \mathcal{C} be the intersection of the cylinders $x^2 + y^2 = 1$ and $y^2 + z^2 = 4$ with $z \geq 0$, oriented counter-clockwise when viewed from above. Evaluate $\int_{\mathcal{C}} \mathbf{F} \cdot d\mathbf{r}$ where $\mathbf{F} = y\mathbf{i} + 2x\mathbf{j} + e^z\mathbf{k}$.

$$\pi \quad 2\pi \quad 0 \quad \sqrt{2} + \pi \quad \sqrt{2}/2 + 2\pi$$

Let S be the sphere $x^2 + y^2 + z^2 = 1$ and let \mathbf{n} be the outward unit normal vector to S . Calculate the flux integral $\iint_S \mathbf{F} \cdot \mathbf{n} \, dS$ where $\mathbf{F}(x, y, z) = xy^2\mathbf{i} + yz^2\mathbf{j} + zx^2\mathbf{k}$.

$4\pi/5$ $2\pi/3$ $\pi/2$ 0 π