

Answer Key 1

MATH 225: Calculus III

Name: \_\_\_\_\_

Exam I Spring 2004

Instructor: \_\_\_\_\_

- 1) There are 10 multiple choice questions worth 6 points each and 3 partial credit problems worth 10 points each. You start with 10 points.
- (2) On the partial credit problems *you must show your work and all important steps to receive credit.*
- (3) Record your answers to the multiple choice problems by **placing an  $\times$  through one letter for each problem on this page.**

You may use a calculator if you wish.

1.  a  b  c  d  •

6.  a  •  c  d  e

2.  a  b  c  •  e

7.  a  b  •  d  e

3.  a  b  c  d  •

8.  a  b  c  d  •

4.  a  b  •  d  e

9.  a  b  •  d  e

5.  •  b  c  d  e

10.  a  b  c  d  •

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number right times 6 = \_\_\_\_\_

11.

12.

13.

You start with: 10 points

Total Score \_\_\_\_\_

1. Determine the cosine of the angle between  $P_0P_1$  and  $P_0P_2$  at  $P_0$  where  $P_0 = (-1, 2, 1)$ ,  $P_1 = (-3, 1, -5)$  and  $P_2 = (-4, 3, -4)$ .

- (a)  $\frac{1}{2}$                       (b) 0                      (c)  $\frac{\sqrt{2}}{2}$                       (d)  $\frac{35}{\sqrt{41}}$                       (e)  $\frac{35}{\sqrt{41}\sqrt{35}}$

2. Find the length of the curve  $\mathbf{r}(t) = \langle t^2, \frac{4}{3}t^{\frac{3}{2}}, t \rangle$  for  $0 \leq t \leq 1$ .

- (a)  $\frac{4}{3}$                       (b) 1                      (c)  $\frac{3}{2}$                       (d) 2                      (e) 4

3. Determine the speed at  $t = 1$  of an object whose position function is  $\mathbf{r}(t) = \langle 2t^3, 3t, 3t^2 \rangle$ .
- (a) 18                      (b) 0                      (c) 8                      (d) 14                      (e) 9

4. Find the distance between the origin and the plane given by the equation  $x + y + z = -1$ .
- (a) 1                      (b)  $\sqrt{3}$                       (c)  $\frac{1}{\sqrt{3}}$                       (d) 0                      (e)  $\frac{2}{\sqrt{3}}$

5. Which of the following points are on the line through the points  $(-1, 1, 0)$  and  $(-1, 5, 7)$ ?

(a)  $(-1, 9, 14)$

(b)  $(-1, 11, 14)$

(c)  $(-1, -4, -7)$

(d)  $(-1, 6, 7)$

(e)  $(-1, 7, 7)$

6. Determine the projection of  $\mathbf{a} = \langle 3, 2, 1 \rangle$  onto  $\mathbf{b} = \langle 2, 2, 1 \rangle$ .

(a)  $\frac{1}{9} \langle 3, 2, 1 \rangle$

(b)  $\frac{11}{9} \langle 2, 2, 1 \rangle$

(c)  $11 \langle 2, 2, 1 \rangle$

(d)  $\frac{11}{9} \langle 3, 2, 1 \rangle$

(e)  $\langle 2, 2, 1 \rangle$

7. Find the domain  $D$  of the function  $f(x, y) = \sqrt{1 - x^2 - y^2}$ .

- (a) all  $(x, y)$  on the plane  
(b)  $\{(x, y) \mid x \leq 1, y \leq 1\}$   
(c) a unit disk  
(d) a unit square  
(e)  $\{(x, y) \mid -1 \leq x \leq 1, -1 \leq y \leq 1\}$

8. A particle moves with position function  $\mathbf{r}(t) = \langle 4 \sin t, 4 \cos t, 3t \rangle$ . Find the tangential and normal components of acceleration.

- (a)  $a_T = 4, a_N = 3$                       (b)  $a_T = 4, a_N = 0$                       (c)  $a_T = 0, a_N = 0$   
(d)  $a_T = \frac{4}{5}, a_N = \frac{4}{5}$                       (e)  $a_T = 0, a_N = 4$

9. Evaluate the integral  $\int (\mathbf{i} + 2t\mathbf{j} + 3t^2\mathbf{k})dt$

(a)  $t + t^2 + t^3 + C$

(b)  $t\mathbf{i} + t^2\mathbf{j} + t^3\mathbf{k}$

(c)  $t\mathbf{i} + t^2\mathbf{j} + t^3\mathbf{k}t + \mathbf{c}$

(d)  $2\mathbf{j} + 6t\mathbf{k} + \mathbf{c}$

(e)  $\mathbf{i} + t^2\mathbf{j} + t^3\mathbf{k}$

10. A point moves in space in such a way that at time  $t$  its position is given by the vector-valued function  $\mathbf{r}(t) = \langle t^2 + 1, 2t^2 - 1, 2 - 3t^2 \rangle$ . At what time does the point hit the plane  $2x + 2y + 3z = 9$ ?

(a) 0

(b) 9

(c)  $\pm 2$

(d)  $\pm \frac{1}{2}$

(e) does not hit

11. Let  $\ell$  be the intersection of the two planes. Find an equation for  $\ell$  in the form of  $\mathbf{r}(t) = \mathbf{r}_0(t) + t\mathbf{v}$ , where two planes are given by equations  $x - y = 1$  and  $x - z = 1$ .



12. Find the unit tangent, the unit normal and binormal vectors for the circular helix  $\mathbf{r}(t) = \langle \cos 3t, \sin 3t, 4t \rangle$ .

13. The initial position and velocity of an object moving with acceleration  $\mathbf{a} = \langle e^t, 0, 0 \rangle$  are  $\mathbf{r}(0) = \langle 2, 3, 2 \rangle$  and  $\mathbf{v}(0) = \langle 1, 1, 1 \rangle$ . Find its position at time  $t$ .