

1. Compute the Wronskian of the functions

$$y_1 = e^{-x} \cos 2x \quad y_2 = e^{-x} \sin 2x$$

- a.  $e^{-x}$       b.  $e^{-2x}$       c. 0      d.  $2e^{-x}$       e.  $2e^{-2x}$

2. Which of the following pair of functions is linearly dependent?

- a.  $f(x) = 1 + 2x$ ,  $g(x) = 1 - 2x$       b.  $f(x) = e^{x+1}$ ,  $g(x) = e^{x-1}$   
c.  $f(x) = e^x$ ,  $g(x) = e^{-x}$       d.  $f(x) = \sin x$ ,  $g(x) = \sin^2 x$   
e.  $f(x) = \sin^2 x$ ,  $g(x) = \cos^2 x$

3. Suppose  $y_1$  and  $y_2$  are two solutions to  $y'' - 2xy' + x^2 y = 0$

Their Wronskian at 0 is equal to 1. Then the Wronskian at 1 is equal to

- a.  $e^1$    b.  $e^{-1}$    c.  $e^2$    d.  $e^{-2}$    e. 0

4. The general solutions of the equation  $y'' - 4y' = 0$  are

- a.  $y = c_1 \cos 2x + c_2 \sin 2x$    b.  $y = c_1 e^{4x} + c_2 x$   
c.  $y = c_1 e^{4x} + c_2$    d.  $y = c_1 e^{-4x} + c_2$   
e.  $y = c_1 e^{-4x} + c_2 x$

5. The solution of the differential equation

$$y'' + 2y' + 2y = 0, \quad y(0) = 0, \quad y'(0) = 1$$

is

- a.  $y = e^{-x} \cos x$    b.  $y = e^x \cos x$    c.  $y = e^x \sin x$

d.  $y = e^{-x} \sin x$

e.  $y = e^{-x} \sin x \cos x$

6. A particular solution to  $y'' - 3y' = x + 2$  should have the following form

a.  $Ax + B$

b.  $x(Ax + B)$

c.  $x^2(Ax + B)$

d.  $e^{3x}(Ax + B)$

e.  $xe^{3x}(Ax + B)$

7. Find the general solution  $y'' + 9y = \sin 3x$

8. Find the general solution of the differential equation

$$y'' + 4y = \sec 2x$$

9. Check that  $y_1 = x$  is a solution of  $x^2 y'' + 2xy' - 2y = 0$  ( $x > 0$ ) and find a second linearly independent solution.