Math 228: Intro to Lin Alg & Diff Eqns

1. Determine which of the following sets S are subspaces of the given vector space V. Be sure to justify your statements.

a)
$$S = \{(1+x, 2+2x) \mid x \in R\}, V = R^2$$

b) Let A be an $m \times n$ matrix. $S = \{ \mathbf{x} \in \mathbb{R}^n \mid A\mathbf{x} = \mathbf{0} \}, V = \mathbb{R}^n$

c) Let
$$f, g \in C[a, b]$$
. $S = \{tf + sg \mid t, s \in R\}, V = C[a, b]$

2. Let $S = \{(0, 1, 1, 1), (1, 1, 1, 0), (1, 0, 0, 1)\}$. Determine whether S is linearly dependent or linearly independent.