## Mathematics 261 – Honors Algebra I Fall Semester 1996 Steve Liedahl

Text: <u>Linear Algebra</u>, 2nd edition, by K. Hoffman and R. Kunze, Prentice Hall, 1971.

## **Comment on Textbook**

It was a privilege to teach from Hoffman and Kunze's text. I followed the chosen sections quite closely (see enclosed Table of Contents), and assigned problems from the text on a weekly basis.

Second-year students need a better grounding in the real spaces  $\mathbf{R}^1, \mathbf{R}^2$ , and  $\mathbf{R}^3$  than this text provides. However, it is written to a high standard, and I think it is appropriate for the course. In choosing the text for a later Math 261 course, this one deserves consideration. Chapter 1. Linear Equations 1

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