

Comments on Maple Problem Set F, Problems 5 and 13

Be sure to read the instructions for the problems carefully and do all parts. You must use Maple on these problems. Do not use `pplane5` to do them. (Of course, if you want to use `pplane5` to help you see what to expect from Maple, that's OK—but the solutions you hand in cannot use `pplane5`).

You can use either **DEplot** (see p. 169 of *Differential Equations with Maple*) or `odeplot` to plot numerical solutions of systems. There are probably other ways as well. Here is how to do this with **odeplot** for a system of two equations. Of course, you have to give specific functions f and g , values for m, n , and you may want to adjust the range of t , and the range of values of a, b .

```
> with(plots):
> sys := diff(x(t),t)=f(x(t),y(t)), diff(y(t),t)=g(x(t),y(t));
> numsol := (a,b) -> dsolve({sys,x(0)=a,y(0)=b},{x(t),y(t)},numeric);
> curve := (a,b,trange) -> odeplot(numsol(a,b),[x(t),y(t)],trange);
> nphase := trange -> display({seq(seq(curve(a,b,trange),a=1..n),b=1..m)});
> nphase(0..10);
```

Problem 5

- You may need to use a fairly large number of points (for example, **numpoints=1000**) in your plot commands to get reasonable plots.
- In part (a), if you get a plot which cannot be correct, please indicate that, and also explain what is wrong with the plot.
- In part (c), you can either differentiate $E(t)$ by hand or have Maple do it. If you have Maple do it, be sure to use $x(t), y(t)$ in your formula for $E(t)$ instead of x, y since otherwise, Maple will think $E(t)$ is a constant function.
- Once you have a formula for the derivative, you need to substitute the formulas for x', y' along a trajectory.
- Parts (b), (f) and (g) require careful thorough explanations.

Problem 13

- In (b) if you don't set a large enough range for t you won't get a very good phase portrait. On the other hand, if it's too large, Maple will have problems doing some of the computations.
- In (b), include both a graphical analysis and a mathematical analysis of stability.