## Math 335, Section 1, Real Analysis Fall 1997 Nancy Stanton

#### Text: Protter & Morrey, A First Course in Real Analysis, 2nd Ed.

I consider the book appropriate for a year long course in real analysis which spends about a semester on analysis in 1 variable and about a semester on analysis in several variables. It has an excellent choice of topics, is well-written, and includes lots of examples. The problems range from easy to medium in level of difficulty. I would use it again. The students find the book hard to read; they would find any analysis book hard to read. Among analysis books, I would rank this as fairly easy.

### Material covered

CHAPTER 1 The Real Number System

- 1.1 Axioms for a Field
- 1.2 Natural Numbers and Sequences
- 1.3 Inequalities
- 1.4 Mathematical Induction

## CHAPTER 2 Continuity and Limits

- 2.1 Continuity
- 2.2 Limits
- 2.3 One-Sided Limits
- 2.4 Limits at Infinity; Infinite Limits
- 2.5 Limits of Sequences

## CHAPTER 3 Basic Properties of Functions on $\mathbb{R}^1$

- 3.1 The Intermediate-Value Theorem
- 3.2 Least Upper Bound; Greatest Lower Bound
- 3.3 The Bolzano-Weierstrass Theorem
- 3.4 The Boundedness and Extreme-Value Theorems
- 3.5 Uniform Continuity
- 3.6 The Cauchy Criterion
- 3.7 The Heine-Borel and Lebesgue Theorems (Lebesgue Theorem skipped)

#### CHAPTER 4 Elementary Theory of Differentiation

- 4.1 The Derivative in  $\mathbf{R}^1$
- 4.2 Inverse Functions in  $\mathbb{R}^1$

#### CHAPTER 5 Elementary Theory of Integration

- 5.1 The Darboux Integral for Functions on R<sup>1</sup>
- 5.2 The Riemann Integral
- 5.3 The Logarithm and Exponential Functions

# CHAPTER 9 Infinite Sequences and Infinite Series

9.1 Tests for Convergence and Divergence

9.2 Series of Positive and Negative Terms; Power Series