

16 Real Analysis II, Spring 1997

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Text: Protter and Morrey, A First Course in Real Analysis, Second Edition

Comments

The book is at an appropriate level for the course. As real analysis books go, it is fairly easy. There is a good range of problems, from very easy to fairly difficult (although few could be described as very difficult). I did not think the chapter on "Integration in \mathbb{R}^n " was very good, but, after doing it and looking at other treatments, I have decided that the Riemann and Darboux integrals are inherently excessively messy in \mathbb{R}^n , and a good treatment of integration in \mathbb{R}^n requires doing the Lebesgue integral, which should not be done at this level. I suggest that the topic be left out of the course. Instead, we could do parts of Chapter 11 (Functions defined by integrals; improper integrals) and the Weierstrass Approximation Theorem. The other chapters I did from the book were good.

A minor caution to anyone using the book: some problems refer back to earlier problems. Occasionally the number of the earlier problem is incorrect (as a result of not changing such references after inserting new problems in the second edition.)

I will use the book again next year.

Syllabus

First Course in Real Analysis
Chapter 6 Elementary Theory of Metric Spaces
6.1 The Schwarz and Triangle Inequalities; Metric Spaces
6.2 Elements of Point Set Topology
6.3 Countable and Uncountable Sets
6.4 Compact Sets and the Heine-Borel Theorem
6.5 Functions on Compact Sets
6.6 Connected Sets
6.7 Mappings from One Metric Space to Another
Chapter 7 Differentiation in \mathbb{R}^n
7.1 Partial Derivatives and the Chain Rule
7.2 Taylor's Theorem; Maxima and Minima
7.3 The Derivative in \mathbb{R}^n
Chapter 8 Integration in \mathbb{R}^n
8.1 Volume in \mathbb{R}^n
8.2 The Darboux Integral in \mathbb{R}^n
8.3 The Riemann Integral in \mathbb{R}^n
Chapter 9 Infinite Sequences and Infinite Series
(9.1--9.2 were done in Math 335)
9.3 Uniform Convergence of Sequences
9.4 Uniform Convergence of Series; Power Series

Chapter 13 Contraction Mappings, Newton's Method, and Differential Equations
 3.1 A fixed Point Theorem and Newton's Method
 3.2 Application of the Fixed Point Theorem to Differential Equations
Chapter 14 Implicit Function Theorems and Lagrange Multipliers
 4.1 The Implicit Function Theorem for a Single Equation
 4.2 The Implicit Function Theorem for Systems