Math 365: Honors Analysis I Name: Quiz 4 November 15, 2000

1. Let $L$ denote the Laplace transform. Prove:
a) $L\left[y^{\prime}\right]=p L[y]-y(0)$
b) $L[x f(x)]=-F^{\prime}(p)$ where $F(p)=L[f(x)]$.
2. Solve the initial value problem $y^{\prime \prime}+2 y^{\prime}+y=x^{2}, y(0)=0, y^{\prime}(0)=0$, a) by direct application of Laplace transforms;
b) by convolution using the impulsive response.
