

Corrections to Third Edition of Pinsky “Partial Differential Equations and Boundary Value Problems with Applications”, 1998. (9 August, 1999)

Page xiv, line 13: Appendices

Page 1, line 7: in the appendices

Page 4, Exercise 2: $u(x, y) = e^{kx}e^{k^2y}$

Page 5, line 2: Newton’s law of gravitational...

Page 5, line 22: $u(x_i; t)$

Page 7, line 21: is *sometimes* called...

Page 9, exercise 1: $u_x(L; t) = 0$

Page 9, exercise 2: $u_x(L; t) = \Phi$

Page 9, exercise 3: $u_x(L; t) = h(T_1 - u(L; t))$

Page 10, line 6: $x^2 + y^2 < R^2$

Page 10, line 13: $t > 0, 0 < x < L$

Page 11, line 11: second item in display should read $\frac{Y''(y)}{Y(y)} = -\lambda$

Page 12, line 17: $(A_1 \sinh kx + \cdots \sin ky)$

Page 15, line 3: $\frac{d}{dx}(e^{\alpha x}) =$

Page 17, line 20: $y^2Y'' + yY' = 0$

Page 17, line 23: $y^2Y'' + yY' + l^2Y = 0$

Page 18, line 5–: $0 = u(0; y) = A_1(\cdots$

Page 18, line 4–: that $A_1 = 0$ and $0 = u(L, y) = A_2 \cdots$

Page 18, line 1–: $A = A_2A_3$ (instead of $A = A_1A_3$)

Page 25, line 15: $\sum_{i=1}^N \|\varphi_i\|^2(c_i - \cdots$

Page 29, line 8: $(1/\sqrt{2\pi}, \sin x/\sqrt{\pi}, \cos x/\sqrt{\pi})$

Page 32, line 7–: ...we have $\langle \varphi, a\psi \rangle = \bar{a} \langle \varphi, \psi \rangle$ for any complex constant

Page 33, Exercise 3: Let \bar{f}

Page 33, Exercise 8: $g(x) = b_1\varphi_1(x) + \dots$

Page 43, line 17: $f_E(x) = f(-x) \quad -L < x < 0$

Page 45, Exercise 10: $-\pi < x < \pi$

Page 46, line 1–: $x' = n\pi x/L$

Page 49, line 6: where $x \in (-\pi, \pi)$

Page 50, lines 2,4,6: $\int_{x_i}^{x_{i+1}}$ instead of $\int_{x_i}^{x_i+1}$ (five different places)

Page 51, line 5: $\cos a \sin b = \frac{1}{2}[\sin(a+b) - \sin(a-b)]$

Page 53, line 8–: Insert “ $\lim_{N \rightarrow \infty}$ ” before $\int_0^\pi D_N(u) du$

Page 56, Exercise 14(a): $f(u) = \dots$

Page 56, Exercise 14(e): If $(N - \frac{1}{2})\pi \leq X \leq (N + \frac{1}{2})\pi$

Page 58, equation (1.3.1) : Insert \dots before $\cos(2n-1)x$

Page 59, last line:

$$\sum_{k=1}^n g(x'_k) \Delta x_k = \dots$$

Page 60, line 2:

$$\frac{2n\pi}{\pi n} \left[\sin(\pi/2n) + \frac{\sin(3\pi/2n)}{3} + \dots \right]$$

Page 65, lines 17,18,19:

$$A'_0 = \frac{1}{2L} \int_{-L}^L \dots$$

$$A'_n = \frac{1}{L} \int_{-L}^L \dots = \frac{n}{L} \int_{-L}^L \dots$$

$$B'_n = \frac{1}{L} \int_{-L}^L \cdots = -\frac{n}{L} \int_{-L}^L \cdots$$

Page 65, line 20:and used the continuity of $f(x)$, $-L < x < L$

Page 66, line 13: $F(-\pi) = F(\pi)$

Page 67, line 3: $\left[\frac{\cos nu - \cos n\pi}{n}\right]$

Page 75, line 2: $(a_n^2 + \cdots$

Page 78, line 11: Change De Moivre's to Euler's

Page 79, line 8: Change De Moivre's to Euler's

Page 79, line 6-: e^{ax} instead of e^{axx}

Page 81, line 4-: $\alpha_0 = [F(L-0) - F(-L+0)]/2L$

Page 83, exercise 5: $\frac{r \sin x}{1+r^2-2r \cos x} = \sum_{n=1}^{\infty} r^n \sin nx$

Page 83, exercise 7: $\lim_{M,N \rightarrow \infty} \sum_{n=-M}^N \alpha_n e^{in\pi x/L}$

Page 83, exercise 7: Try example 1.1.4 at $x = 0$

Page 85, line 20: $0 = A \cos(L\sqrt{\lambda}) + \cdots$

Page 87, line 3 of Solution of Example 1.6.3: $= A(1 + hL)$

Page 87, lines 6-7 of Solution of Example 1.6.3: $0 = h(Ae^{\mu L} + Be^{-\mu L}) + \cdots$

Page 87, line 10 of Solution of Example 1.6.3: $B\sqrt{\lambda}$

Page 90, Last two lines:

$$\cos \alpha (A \sinh \mu a + \cdots + B \mu \sinh \mu a) = 0$$

$$\cos \beta (A \sinh \mu b + \cdots + \mu B \sinh \mu b) = 0$$

Page 92, line 16: This is in the interval $0 < L\sqrt{-\lambda} < \sqrt{|\cot \alpha \cot \beta|}$

Page 92, lines 18-19: The first one satisfies $0 < L\sqrt{-\lambda_1} < \sqrt{|\cot \alpha \cot \beta|}$ while the second one satisfies $L\sqrt{-\lambda_2} > \sqrt{|\cot \alpha \cot \beta|}$

Page 93, bulleted summary:

Second bullet should read:This satisfies $0 < L\sqrt{-\lambda_1} < \sqrt{|\cot \alpha \cot \beta|}$

Third bullet should read:..... The first one satisfies $0 < L\sqrt{-\lambda_1} < \sqrt{|\cot \alpha \cot \beta|}$ while the second one satisfies $L\sqrt{-\lambda_2} > \sqrt{|\cot \alpha \cot \beta|}$

Page 99, line 4–: gradu (decrease space)

Page 100, line 11–: delete minus sign before “div”

Page 101, line 12: When $x_2 \rightarrow x_1$, the *integrand* tends to....

Page 101, line 13: ...resulting integral tends to $q_x^x(x_1, y_1, z_1)$

Page 103, line 4: $-hT_1$ (delete /k)

Page 103, line 5: $-kB$ (insert minus sign)

Page 105, line 22: $\sqrt{\pi K \tau}$

Page 108, Exercise 3, lines 2-3: $\dots + h(u - T_0)](x, y, L) = 0$

Page 113, line 5–: $O(e^{-at})$ (change 0 to O)

Page 120, exercise 6, line 2: $u_z(L : t) = 0$

Page 123, line 6–: $U''(z) - \sum_{n=1}^{\infty}$ (change = to -)

Page 125, line 14–: $u_z(L; t) = 0$

Page 125, line 1–: (4') : $v(z; 0) = T_3 - T_1$

Page 126, line 10–: $B\sqrt{\lambda} \cos L\sqrt{\lambda}$

Page 127, example 2.3.2: ...where h, T_1, T_2 and T_3 are...

Page 127, line 1–: $U(z) = T_1 + hz(T_2 - T_1)/(1 + hL)$ (change t_2 to T_2)

Page 130, line 3–: f_n , and $u_n(t)$ are obtained....

Page 131, line 4: $u_n(0) = f_n$

Page 131, line 6: $u_n(t) = f_n e^{-\lambda_n K t} + \dots$

Page 131, line 10–: $\cos \alpha \sin \beta + \sin \alpha \cos \beta + \cos \alpha \cos \beta \neq 0$

Page 136, line 1: Should read

$$-T^-(a:t) \frac{(\partial \mathbf{r} / \partial s)(a;t)}{|\partial \mathbf{r} / \partial s)(a;t)|} = \dots$$

(add minus sign and change b to a in three places

Page 154, line 14- : $\sum_{m,n=1}^{\infty}$ instead of single sum

Page 154, line 10- : $\sum_{m,n=1}^{\infty}$ instead of single sum

Page 157, line 11-: $\sum_{m,n=1}^{\infty}$ instead of single sum

Page 158. lines 13, 17, 19,22: $\sum_{m,n=1}^{\infty}$ instead of single sum

Page 160, line 8: $\sum_{m,n=1}^{\infty}$ instead of single sum

Page 163, line 16 of table: $2^3 \cdot 5$

Page 165, line 3-: $x = L_1$

Page 172, line 4-: $u_{\varphi\varphi}$ at end

Page 175, solution of example 3.1.3 :

$$-k \frac{\partial u}{\partial \rho} |_{\rho=\rho_2} = \frac{-k}{\rho_2} \frac{T_2 - T_1}{\ln(\rho_2/\rho_1)}$$

Page 178. line 15-: $R^{-n} B_n = \dots$

Page 187, line 3: $\frac{a_0}{\rho\sqrt{\lambda}} \sum \dots$

Page 189, line 4-: $e^{-i\theta}$ instead of $e^{i\theta}$

Page 189, line 3-: $= - \int_0^{\pi} \dots$

Page 190, line 8: $= -\frac{x}{m}$

Page 191, line 13; This is a first-order linear equation for v' , which may be solved.....

Page 196, lines 1-2: $\theta(\rho)$ is unbounded when $\rho \rightarrow \infty$.

Page 197, line@: $= +R(x) \dots$ and $\cos \beta J_m(x) + x \sin x J'_m(x) = 0$

Page 198, line 5: Add $\lambda = x_n^2$ at end of line

Page 200, line 1: ...use the formulas (3.2.18)-(3.2.19)....

Page 201, line 7-: $\beta = 0$

Page 202, line 11: $\int_0^1 x J_0(x x_n)^2 dx$

Page 204, line 3: **jj[3.5, 4]**

Page 204, line 5: **jj[3.8, 3.85]**

Page 211, line 12-: initial conditions (3.3.2)-(3.3.3)

Page 213, line 9-: and $A_{0n} = 0$ for $n > 0$, while...

Page 218, line 8: $\beta = 0$

Page 219, line 12: $U(\rho_{max}) = T_1$

Page 221, line 14 [will check dimensions here and elsewhere]

Page 222, line 3: $-\pi \leq \varphi \leq \pi$

Page 223: lines 6,11,12, 14,15: Change Φ to R in each case

Page 223, line 16: chnage $R_2^2 - R_1^2$ to $\rho_2^2 - \rho_1^2$

Page 225, line 8: $\lambda = i\omega/K$

Page 228, line 20: delete $-m^2$

Page 232, line 14: $1 = \frac{8}{\pi} \dots$

Page 238, line 1: $w_r = r u_r + u$

Page 241, line 10: $f(r) = T_2$

Page 244, line 8: $ka\mu/(k - ah)$

Page 244, line 5-: $r f(r) - W(r)$

Page 247, line 10-: change L to a in two places

Page 247, line 6-: $(2aC/n\pi)$

Page 247, line 4-: change L to a

Page 259, line 6: $[(1 - a^2)P'_k(a) - (1 - b^2)P'_k(b)]$

Page 280, line 11–: $e^{-ia\mu}F(\mu)$ is the Fourier....

Page 286, line 3–:satisfies $\int_0^\infty |F_s(\mu)| d\mu < \infty$

ANSWERS

Page 503, sec 0.2.3, exercise 1(d): $Y' + (\lambda - 1)Y = 0$

Page 504, Exercise 5: first line should read:

$$\lambda < 0 : u(x, y) = [A_1 \cos(\sqrt{-\lambda} \ln |x|) + A_2 \sin(\sqrt{-\lambda} \ln |x|)](A_3 e^{y\sqrt{\lambda}} + A_4 e^{-y\sqrt{\lambda}})$$

Page 504, solution of Exercise no. 2 in section 0.2.4: should be $A_n \sin(\dots)$ instead of $A_n \cos(\dots)$

Page 504, Exercise 1(d) in section 0.3: answer to part (d) should be (7)

Page 505, Exercise 5 in section 1.1: should be $\frac{1}{2} - \frac{1}{2} \cos(4x)$

Page 505, Exercise 6 in section 1.1: should be $\frac{1}{2} \cos 3x + \frac{3}{4} \cos(4x)$

Page 505, line 19 (exercise 16(c)): change $L/n\pi$ into $n\pi/L$ in the denominator

Page 507, line –2: Change Φ_0 to Φ .

Page 511, Section 3.3, Exercise 1: $U(\rho) = (g/4c^2)(\rho^2 - a^2)$

Page 511, line 1–: exercise 5, last part is incorrect formula for A_n . Need $A_n = \frac{2}{acx_n J_1(x_n)^2} \int_0^R \dots$

End of corrections, August 9, 1999