

18 Topology
Spring 1998
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Text: Differential Topology by Guillemin and Pollock

Actually, the first half of the semester was spent on point-set topology for subsets of Euclidean space, and we didn't use a book. I ended up writing summaries of the main ideas and posting them on the web page for the course. I had planned to work through a bit of the next book very slowly, but we ended up doing less than I had hoped.

Particular comments about the book: this is a very hard book, especially for weak math majors. It requires a certain level of mathematical sophistication; students who have carefully read parts of a real math book will have a good grounding, but it didn't seem that any of the students in the class had this grounding (even some of the stronger students). I think this book would be suitable for a strong group of senior math majors; for a group of mixed ability levels, I would use something else. (Various people have suggested: M. Henle, "A combinatorial introduction to topology", C.T.C Wall, "A geometric introduction to topology", E. Bloch, "A first course in geometric topology and differential geometry")
But I can't really vouch for any of these. Bloch's is the newest, at least well tested.)

Material covered:

Open and closed sets in Euclidean space.

Countable and uncountable sets.

Naive topological spaces (Definition: A "naive topological space" is a subset of \mathbb{R}^n for some n .)

Properties of open sets in \mathbb{R}^n , properties of closed sets.

Open, closed subsets in an arbitrary naive topological space.

Connectedness.

Limit points.

Continuous functions.

meomorphism.

ages, preimages, continuity.

en covers, compact sets.

space-filling curve.

urfaces.

om the text:

ction 1.1 (definition of manifold)

ction 1.2 (derivative, tangent space)

(both in quite a bit of detail)

ction 1.4 (the "preimage theorem" in particular)

ctions 1.5 and 1.6 (the definition of transversality in particular)

(briefly)