## AME 20214 Homework 3

Due: Thursday, 13 September 2012, in class

1. (60) Consider the standard model, which can be derived from Newton's second law of motion, of a linear mass-spring system:

$$m\frac{d^2y}{dt^2} + ky = 0, \qquad y(0) = y_o, \qquad \frac{dy}{dt}\Big|_{t=0} = 0.$$

Here y is the distance with units of m, t is the time with units of s, m is the mass with units of kg, and k is the spring constant with units of N/m. The term  $y_o$  is the initial displacement with units of m. The exact solution is easily seen by direct substitution to be

$$y(t) = y_o \cos\left(\sqrt{\frac{k}{m}}t\right).$$

If we define the velocity v to be v = dy/dt, we can re-write the governing equation as a system of two first order differential equations:

$$\frac{dy}{dt} = v, \qquad y(0) = y_o,$$
$$\frac{dv}{dt} = -\frac{k}{m}y, \quad v(0) = 0.$$

This system can be simulated computationally using the Euler method for a system. Simple discretization of the system shows

$$\frac{y_{n+1} - y_n}{\Delta t} = v_n,$$
$$\frac{v_{n+1} - v_n}{\Delta t} = -\frac{k}{m}y_n.$$

For  $m = 1 \ kg$ ,  $k = 9 \ N/m$ ,  $y_o = 1 \ m$ ,  $t \in [0, 10 \ s]$ , numerically estimate y(t) with the Euler method, embodied in a Fortran code. For  $\Delta t = 0.01 \ s$ , plot on the same plot the exact solution and your computational estimate for  $t \in [0, 10 \ s]$ . You can choose to copy and paste your Fortran output into matlab for plotting, or you can read ahead and learn how to read and write from files. Choose your favorite precision, and plot on a log-log scale the error at  $t = 10 \ s$  as a function of  $\Delta t$ . Comment on the stability of the method as a function of  $\Delta t$ .

- 2. (20) Create a home page in your Notre Dame-maintained space on the world wide web. If you don't know how to make a home page, I will give a short explanation in class. It takes about five minutes. If you want to do this on your own, you can go to the AME 20214 homepage, documents section. Once there, *right* click on the file Template for the file index.html. Next choose browser option "View Source," usually found under the "View" toolbar on your browser (under "Develop" in Safari). The next step is important. Save the raw text file, which has the temporary placeholder name of index.template.html, as the permanently named index.html in your netfile space *in* the directory www. Note that the netfile space is the Notre Dame default for student web pages, not afs space. Test to see if it works, then use a text editor to modify it appropriately so that your name is identified on the home page in whatever fashion you see fit. Add any æesthetics you wish.
- 3. (20) Retrieve document sample.tex and sample.figure.eps from the "documents" link at the course home page,

http://www.nd.edu/~powers/ame.20214/,

edit it to add your name, process it with a LATEX processor, convert it to .pdf format, and print a copy of the compiled file. Use instead sample2.tex and sample\_figure.pdf if you intend to use pdflatex. Post your .pdf file on your Notre Dame personal web page.

Be sure to follow the homework format specified in the course syllabus.