

AME 538

Homework 1

Due: Friday, 25 August 2000, in class

1. Respond to my e-mail message if you received it.
2. Retrieve document `sample.tex` and `sample.figure` from the “documents” link under
<http://www.nd.edu/~powers/ame.538>,
edit it to add your name, and print a copy of the compiled file. You should save `sample.figure` as `sample.figure.eps`
3. Consider a flow which has variation in one spatial dimension, denoted by x , and time, denoted by t . The material derivative (also known as the total derivative, substantial derivative, or derivative following a fluid particle) of an arbitrary flow variable $f(x, t)$, where f could represent, e.g. temperature, pressure, density, etc., is defined as

$$\frac{df}{dt} = \frac{\partial f}{\partial t} + u \frac{\partial f}{\partial x}.$$

Show that the material derivative is invariant under a Galilean change of reference frame (as it must be in the context of Newtonian, but not Einsteinian, physics). In a Galilean transformation we map $(x, t) \rightarrow (x', t')$ and $u \rightarrow u'$ via the mappings

$$\begin{aligned}x' &= x - Vt, \\t' &= t, \\u' &= u - V.\end{aligned}$$

Here V is a constant velocity of the moving reference frame.