

AME 538
Examination 2
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1. (30) Air, with $\gamma = 7/5$, $R = 287 \text{ J/kg/K}$, flows isentropically in a variable area duct. At station 1, the static temperature, static pressure, and velocity are 400 K , 100 kPa , and 300 m/s . Find the static temperature, static pressure, and velocity at a point downstream where the duct has twice the area.
2. (30) Air, with $\gamma = 7/5$, $R = 287 \text{ J/kg/K}$ is initially at rest in a cylinder at $T = 300 \text{ K}$, $P = 100 \text{ kPa}$. At $t = 0$, a piston initially at $x = 0$ is suddenly retracted at velocity 150 m/s . Determine the final temperature after the rarefaction, and sketch the process in an $x - t$ plane.
3. (40) Consider a cylinder of radius c in a two-dimensional, inviscid, incompressible flow field, with far field velocity U in the x direction, far-field pressure P_o , and density ρ . Find the amount of circulation Γ which is necessary to merge the two stagnation points to a single point. Find the pressure at the stagnation point. Sketch the streamlines and lines of constant potential.