

The Dynamics of Unsteady Detonation in Ozone

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Motivation

- Computational tools are critical in design of aerospace vehicles which employ high speed reactive flow.
- Steady wave calculations reveal **sub-micron scale structures** in detonations with detailed kinetics (Powers and Paolucci, *AIAA J.*, 2005).
- Small structures are continuum manifestations of molecular collisions.
- We explore the transient behavior of detonations with ***fully resolved*** detailed kinetics.

Verification and Validation

- *verification*: solving the equations right (math).
- *validation*: solving the right equations (physics).
- Main focus here on verification
- Some limited validation possible, but detailed validation awaits more robust measurement techniques.
- Verification and validation always necessary but never sufficient: finite uncertainty must be tolerated.

Model: Reactive Euler Equations

- one-dimensional,
- unsteady,
- inviscid,
- detailed mass action kinetics with Arrhenius temperature dependency,
- ideal mixture of calorically imperfect ideal gases

Model: Reactive Euler PDEs

$$\begin{aligned}\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x} (\rho u) &= 0, \\ \frac{\partial}{\partial t} (\rho u) + \frac{\partial}{\partial x} (\rho u^2 + p) &= 0, \\ \frac{\partial}{\partial t} \left(\rho \left(e + \frac{u^2}{2} \right) \right) + \frac{\partial}{\partial x} \left(\rho u \left(e + \frac{u^2}{2} + \frac{p}{\rho} \right) \right) &= 0, \\ \frac{\partial}{\partial t} (\rho Y_i) + \frac{\partial}{\partial x} (\rho u Y_i) &= M_i \dot{\omega}_i, \\ p &= \rho \mathcal{R} T \sum_{i=1}^N \frac{Y_i}{M_i}, \\ e &= e(T, Y_i), \\ \dot{\omega}_i &= \dot{\omega}_i(T, Y_i).\end{aligned}$$

Computational Methods

- Steady wave structure
 - LSODE solver with IMSL DNEQNF for root finding
 - Ten second run time on single processor machine.
 - see Powers and Paolucci, *AIAA J.*, 2005.
- Unsteady wave structure
 - Shock fitting coupled with a high order method for continuous regions
 - see Henrick, Aslam, Powers, *J. Comp. Phys.*, 2006, for full details on shock fitting

Outline of Shock Fitting Method

- Transform from lab frame to shock-attached frame
 - example mass equation becomes

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x} (\rho (u - D)) = 0$$

- In interior, approximate spatial derivatives with fifth order Lax-Friedrichs discretization
- At shock boundary, one-sided high order differences are utilized

Outline of Shock Fitting Method

- Note that some form of an approximate Riemann solver must be used to determine the shock speed, D , and thus set a valid shock state
- At downstream boundary, a zero gradient (constant extrapolation) approximation is utilized
- Fifth order Runge-Kutta time integration is employed

Ozone Reaction Kinetics

Reaction	a_j^f, a_j^r	β_j^f, β_j^r	E_j^f, E_j^r
$O_3 + M \rightleftharpoons O_2 + O + M$	6.76×10^6	2.50	1.01×10^{12}
	1.18×10^2	3.50	0.00
$O + O_3 \rightleftharpoons 2O_2$	4.58×10^6	2.50	2.51×10^{11}
	1.18×10^6	2.50	4.15×10^{12}
$O_2 + M \rightleftharpoons 2O + M$	5.71×10^6	2.50	4.91×10^{12}
	2.47×10^2	3.50	0.00

see Margolis, *J. Comp. Phys.*, 1978, or Hirschfelder, *et al.*,
J. Chem. Phys., 1953.

Validation: Comparison with Observation

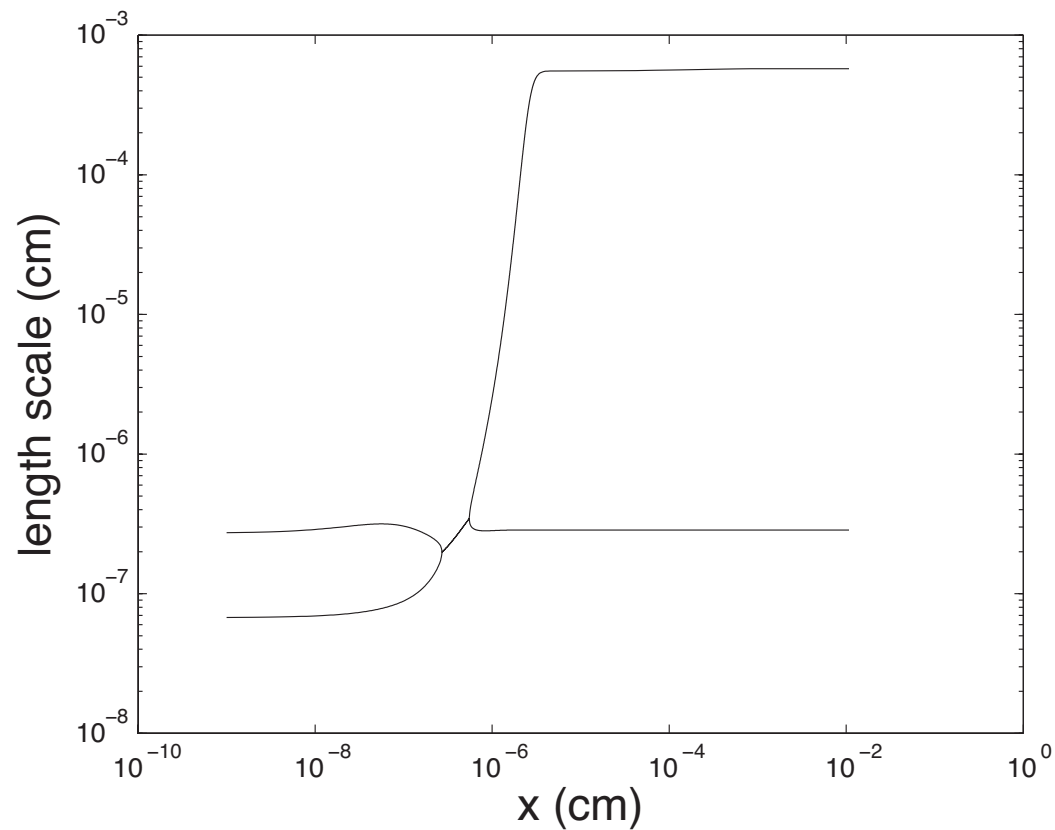
- Streng, *et al.*, *J. Chem. Phys.*, 1958.
- $p_o = 1.01325 \times 10^6 \text{ dyne/cm}^2$, $T_o = 298.15 \text{ K}$,
 $Y_{O_3} = 1$, $Y_{O_2} = 0$, $Y_O = 0$.

Value	Streng, <i>et al.</i>	this study
D_{CJ}	$1.863 \times 10^5 \text{ cm/s}$	$1.936555 \times 10^5 \text{ cm/s}$
T_{CJ}	3340 K	3571.4 K
p_{CJ}	$3.1188 \times 10^7 \text{ dyne/cm}^2$	$3.4111 \times 10^7 \text{ dyne/cm}^2$

Slight overdrive to preclude interior sonic points.

Stable Strongly Overdriven Case: Length Scales

$$D_o = 2.5 \times 10^5 \text{ cm/s.}$$



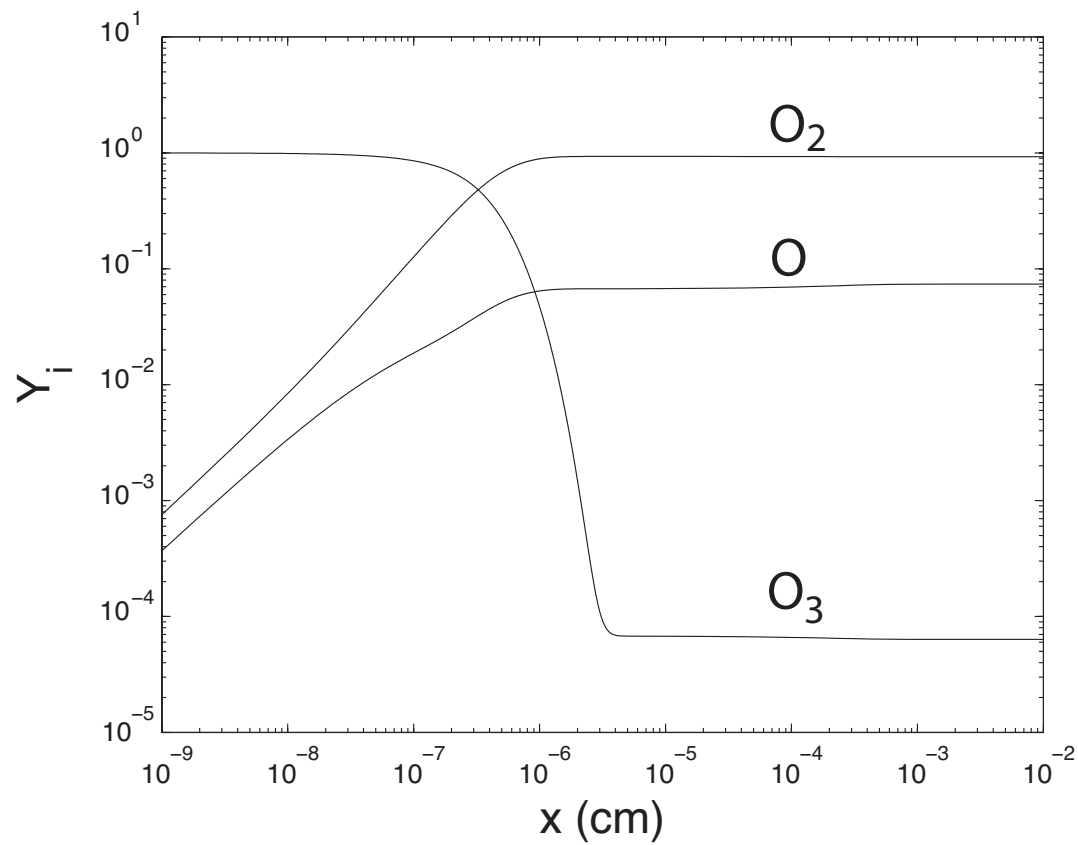
Mean-Free-Path Estimate

- The mixture mean-free-path scale is the cutoff *minimum* length scale associated with continuum theories.
- A simple estimate for this scale is given by *Vincenti and Kruger, '65*:

$$\ell_{mfp} = \frac{M}{\sqrt{2}\mathcal{N}\pi d^2\rho} \sim 10^{-7} \text{ cm.}$$

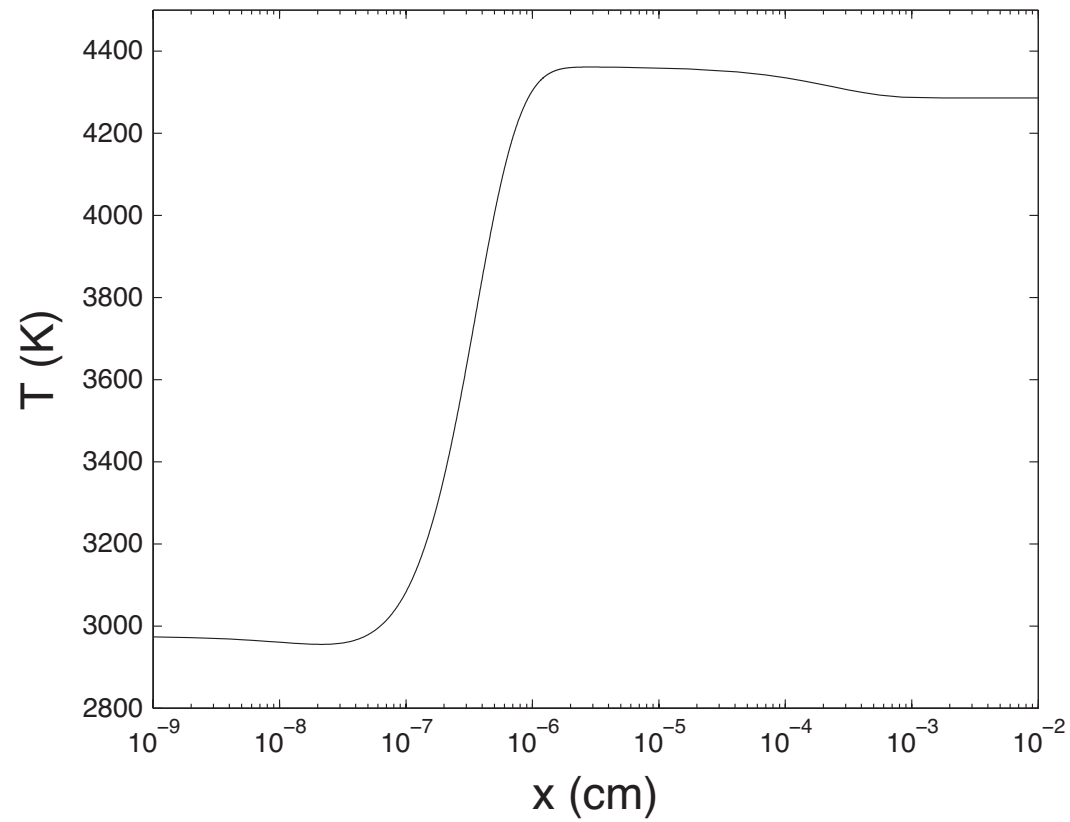
Stable Strongly Overdriven Case: Mass Fractions

$$D_o = 2.5 \times 10^5 \text{ cm/s.}$$



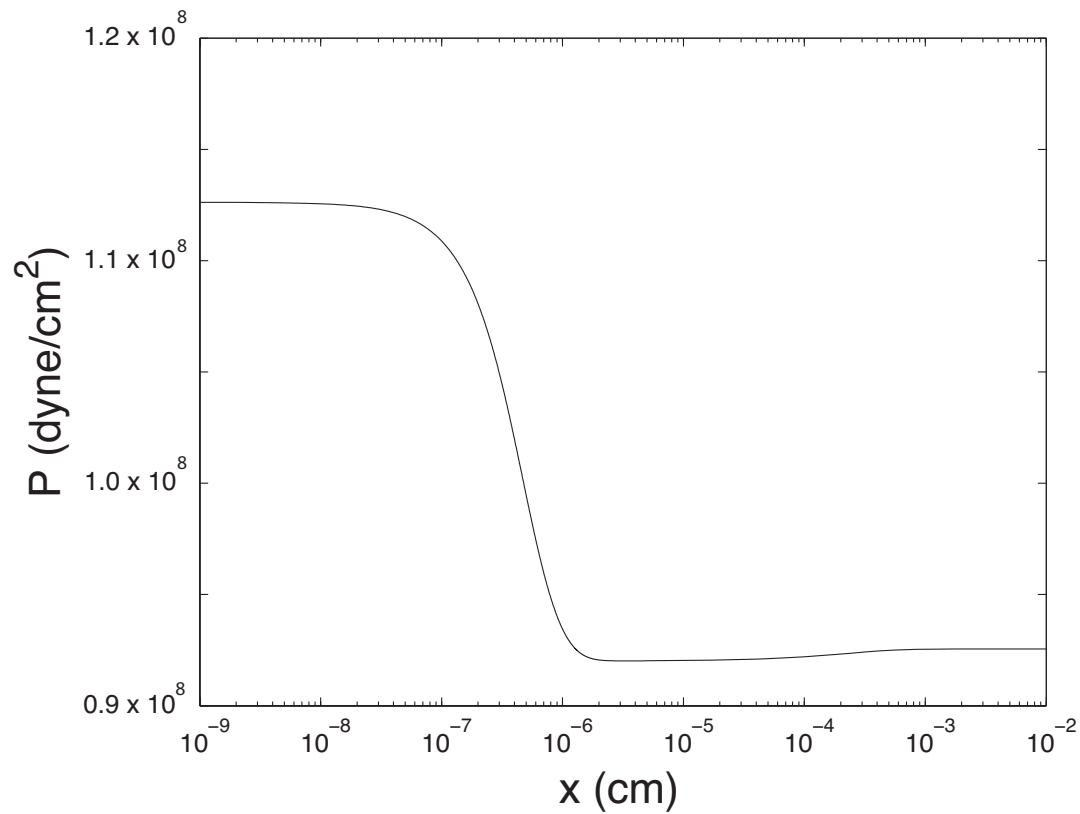
Stable Strongly Overdriven Case: Temperature

$$D_o = 2.5 \times 10^5 \text{ cm/s.}$$



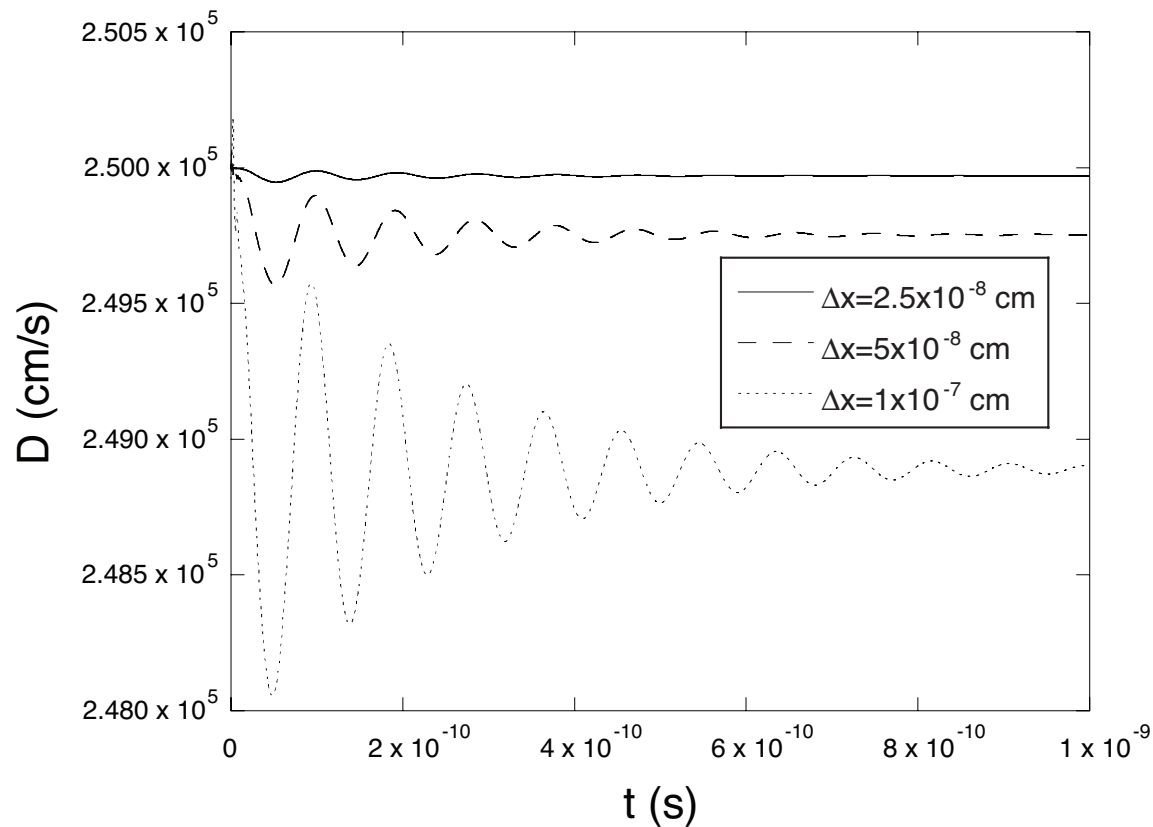
Stable Strongly Overdriven Case: Pressure

$$D_o = 2.5 \times 10^5 \text{ cm/s.}$$

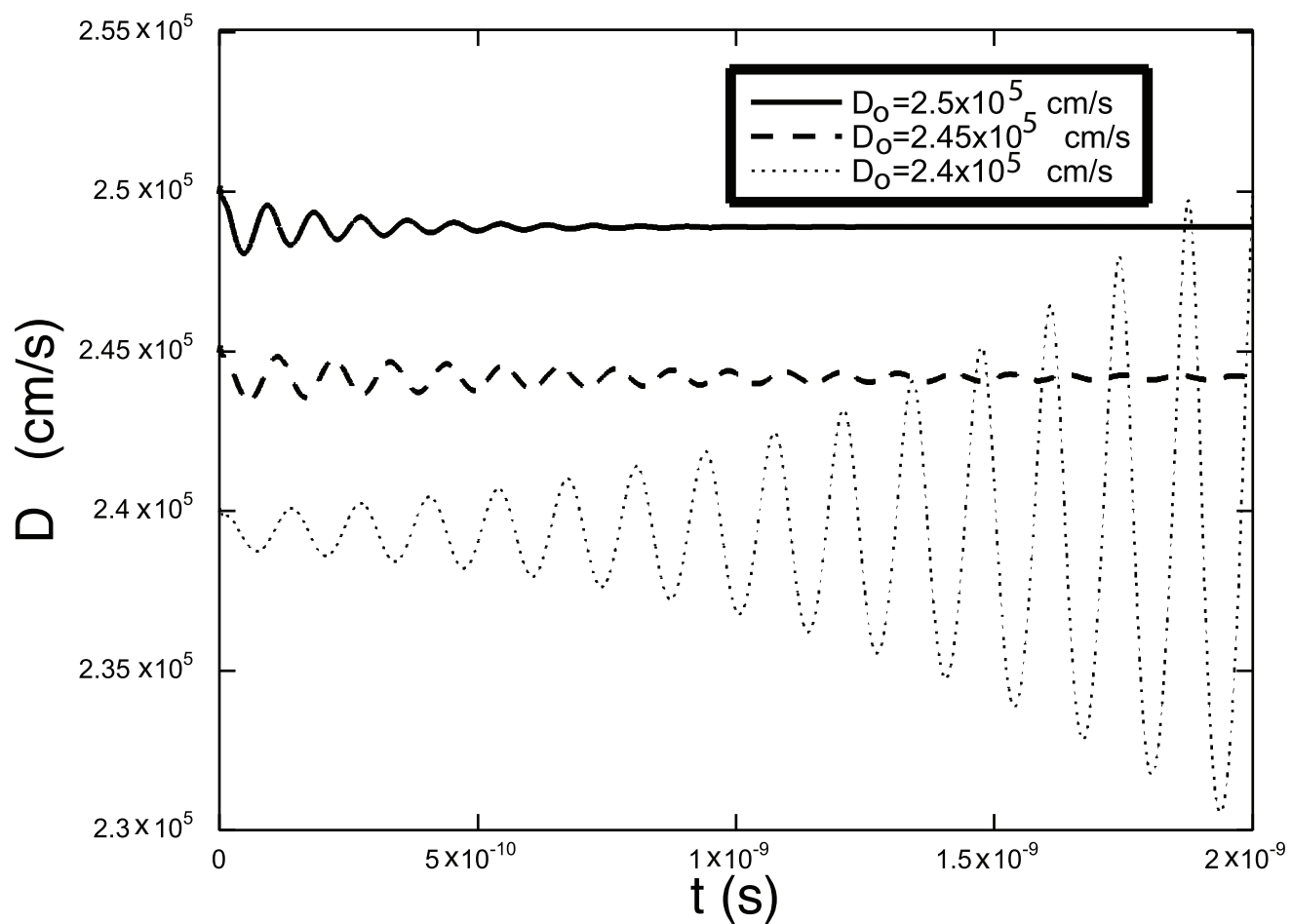


Stable Strongly Overdriven Case: Transient Behavior for Various Resolutions

Initialize with steady structure of $D_o = 2.5 \times 10^5 \text{ cm/s}$.

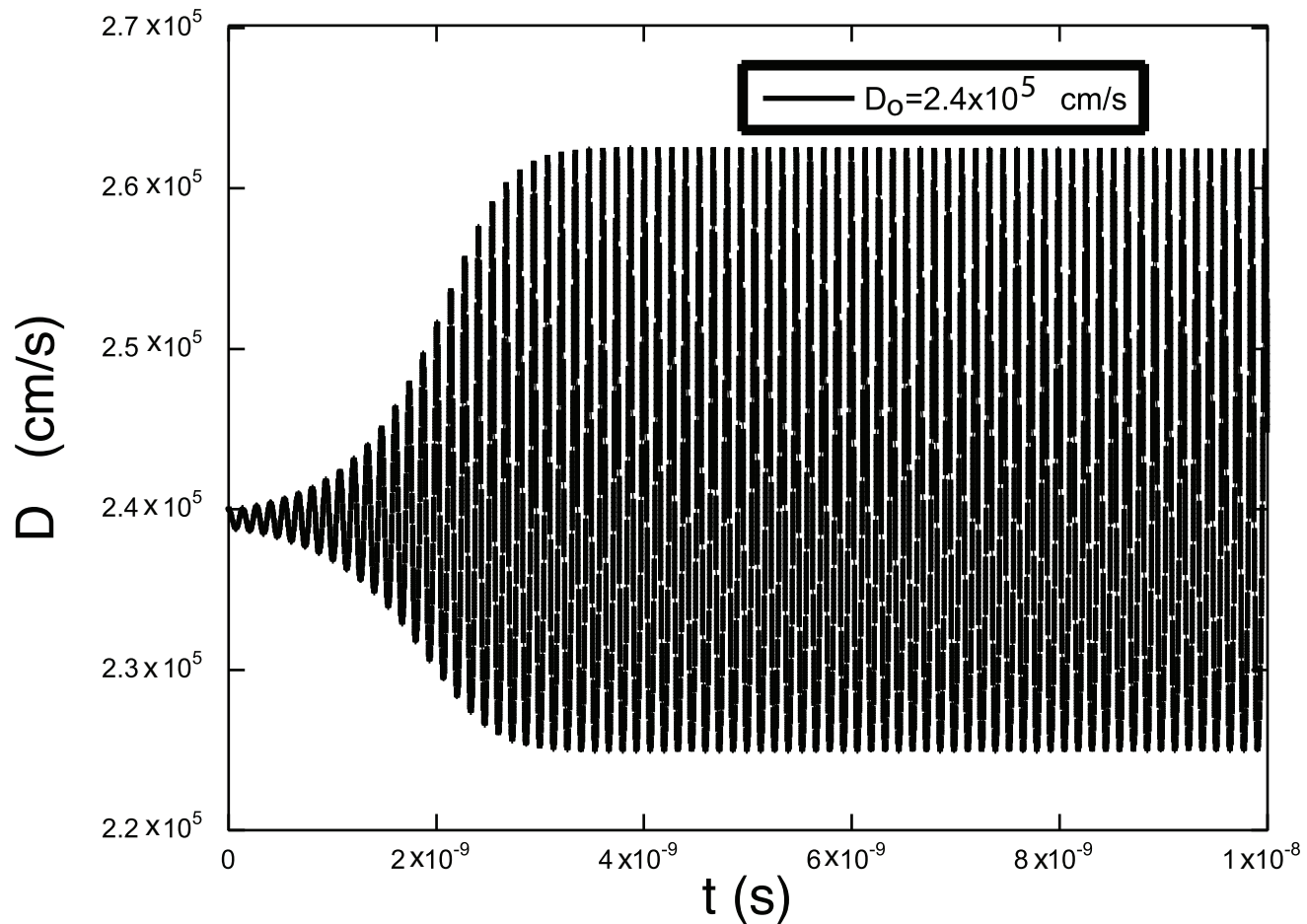


3 Cases Near Neutral Stability: Transient Behavior



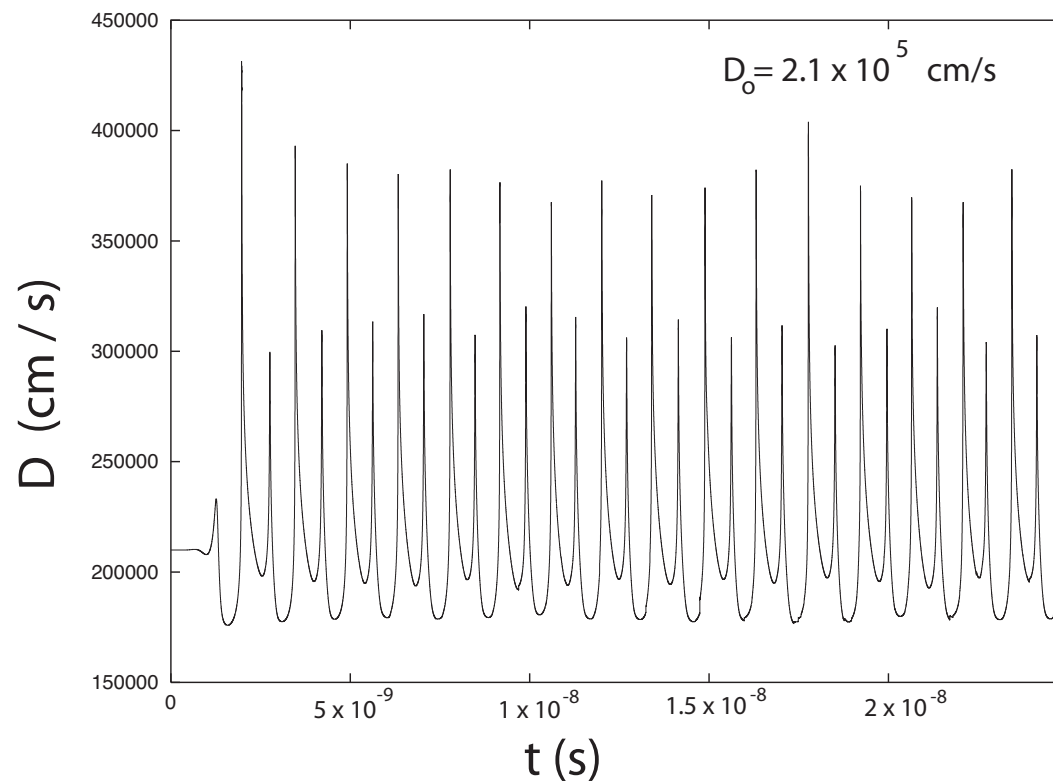
Slightly Unstable Case: Transient Behavior

Initialized with steady structure, $D_o = 2.4 \times 10^5 \text{ cm/s}$.

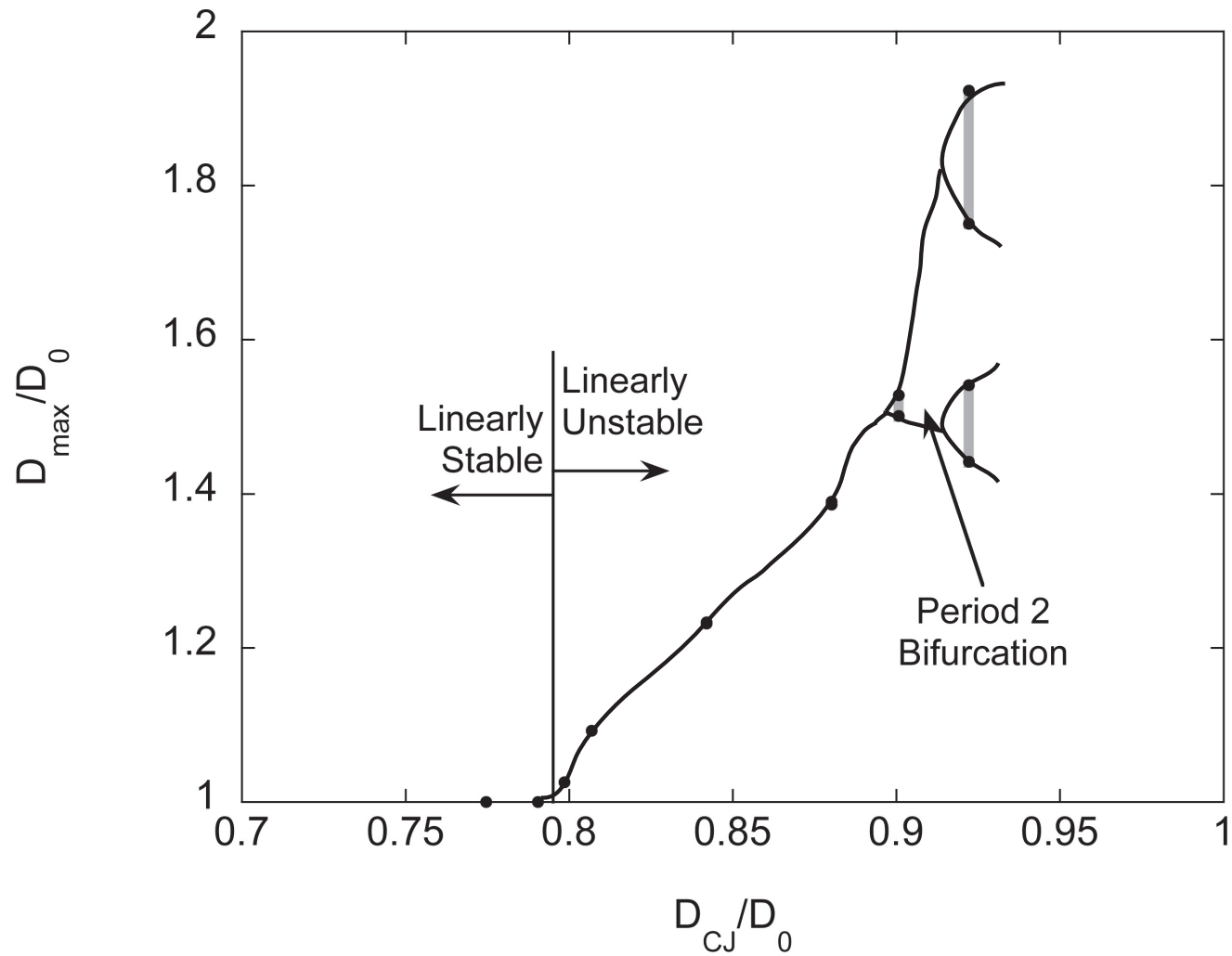


Case After Bifurcation: Transient Behavior

Initialized with steady structure of $D_o = 2.1 \times 10^5 \text{ cm/s}$.



Long Time D_{max}/D_0 versus D_{min}/D_0



Effect of Resolution on Unstable Moderately Overdriven Case

Δx	Numerical Result
$1 \times 10^{-7} \text{ cm}$	Unstable Pulsation
$2 \times 10^{-7} \text{ cm}$	Unstable Pulsation
$4 \times 10^{-7} \text{ cm}$	Unstable Pulsation
$8 \times 10^{-7} \text{ cm}$	O_2 mass fraction > 1
$1.6 \times 10^{-6} \text{ cm}$	O_2 mass fraction > 1

- Algorithm failure for insufficient resolution
- At low resolution, one misses critical dynamics

Conclusions

- Unsteady detonation dynamics can be accurately simulated when sub-micron scale structures admitted by detailed kinetics are captured with ultra-fine grids.
- Shock fitting coupled with high order spatial discretization assures numerical corruption is minimal.
- Predicted detonation dynamics consistent with results from one-step kinetic models.
- At these length scales, diffusion will play a role and should be included in future work.