

Answer Key 1

MATH 10560: Calculus II

Practice Final 2

December 17, 2009

Record your answers to the multiple choice problems by placing an \times through one letter for each problem on this page. There are 20 multiple choice questions worth 6 points each. You start with 30 points.

You may not use a calculator.

1. a b c d e

11. a b c d e

2. a b c d e

12. a b c d e

3. a b c d e

13. a b c d e

4. a b c d e

14. a b c d e

5. a b c d e

15. a b c d e

6. a b c d e

16. a b c d e

7. a b c d e

17. a b c d e

8. a b c d e

18. a b c d e

9. a b c d e

19. a b c d e

10. a b c d e

20. a b c d e

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1. a b c d e11. a b c d e2. a b c d e12. a b c d e3. a b c d e13. a b c d e4. a b c d e14. a b c d e5. a b c d e15. a b c d e6. a b c d e16. a b c d e7. a b c d e17. a b c d e8. a b c d e18. a b c d e9. a b c d e19. a b c d e10. a b c d e20. a b c d e

1. Determine which expression gives the length of the curve $x = t - \ln(t)$, $y = t + \ln(t)$, $1 \leq t \leq 2$.

(a) $\int_1^2 \sqrt{1 + \left(1 + \frac{1}{t}\right)^2} dt$

(b) $\int_1^2 \sqrt{2 + \frac{4}{t} + \frac{2}{t^2}} dt$

(c) $\int_1^2 \sqrt{1 + \left(1 - \frac{1}{t}\right)^2} dt$

(d) $\int_1^2 \sqrt{2t^2 + 2\ln(t)^2} dt$

(e) $\int_1^2 \sqrt{2 + \frac{2}{t^2}} dt$

2. Determine which phrase applies to the series $\sum_{n=2}^{\infty} (-1)^n \frac{\ln(n)}{n^2}$

(a) *diverges by the Divergence Test*

(b) *converges absolutely*

(c) *converges by the Ratio Test*

(d) *converges conditionally*

(e) *diverges by the Integral Test*

3. Evaluate $\int_0^{\infty} \frac{e^x}{e^{2x} + 1} dx$

(a) *diverges*

(b) $\pi/2$

(c) π

(d) $\pi/4$

(e) 2π

4. At 1:00 PM a bacteria colony had a population of 1000. At 1:30 PM the number was 1500. Assuming the population grows exponentially, determine its size at 2:00 PM.

(a) 1750

(b) 2000

(c) 2500

(d) 2750

(e) 2250

5. Use power series to evaluate $\int \ln(1 - x^3) dx$.

$$(a) C - \frac{1}{3}x^3 - \frac{1}{2 \cdot 6}x^6 - \frac{1}{3 \cdot 8}x^8 - \frac{1}{4 \cdot 10}x^{10} - \dots$$

$$(b) C - \frac{1}{4}x^4 - \frac{1}{2 \cdot 5}x^5 - \frac{1}{3 \cdot 6}x^6 - \frac{1}{4 \cdot 7}x^7 - \dots$$

$$(c) C - \frac{1}{2}x^2 - \frac{1}{3 \cdot 5}x^5 - \frac{1}{4 \cdot 8}x^8 - \frac{1}{5 \cdot 11}x^{11} - \dots$$

$$(d) C - x^3 - \frac{1}{2}x^6 - \frac{1}{3}x^9 - \frac{1}{4}x^{12} - \dots$$

$$(e) C - \frac{1}{4}x^4 - \frac{1}{2 \cdot 7}x^7 - \frac{1}{3 \cdot 10}x^{10} - \frac{1}{4 \cdot 13}x^{13} - \dots$$

6. Compute the second degree Taylor polynomial for $f(x) = x \cos(x)$ at $a = \frac{\pi}{2}$.

$$(a) \left(x - \frac{\pi}{2}\right) - \frac{1}{2}\left(x - \frac{\pi}{2}\right)^2$$

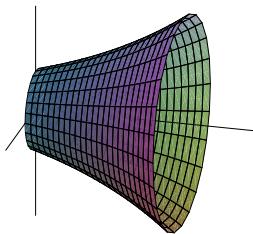
$$(b) \frac{\pi}{2}\left(x - \frac{\pi}{2}\right) - \frac{\pi}{4}\left(x - \frac{\pi}{2}\right)^2$$

$$(c) x - \frac{1}{2}x^3$$

$$(d) -\frac{\pi}{2}\left(x - \frac{\pi}{2}\right) - \left(x - \frac{\pi}{2}\right)^2$$

$$(e) -\frac{\pi}{2}x + x^2$$

7. Determine which integral gives the area of the surface obtained by rotating $y = e^x$, $0 \leq x \leq 1$, about the x -axis.



(a) $2\pi \int_0^1 x\sqrt{1+e^{2x}} dx$

(b) $2\pi \int_0^1 e^x dx$

(c) $2\pi \int_0^1 \sqrt{1+e^x} dx$

(d) $2\pi \int_0^1 e^x \sqrt{1+e^{2x}} dx$

(e) $2\pi \int_0^1 xe^x dx$

8. Evaluate $\int \frac{1}{(x^2 + 4)^{3/2}} dx$

(a) $\ln |x + \sqrt{x^2 + 4}| + C$

(b) $\frac{1}{2\sqrt{x^2 + 4}} + C$

(c) $\frac{\sqrt{x^2 + 4}}{4x} = C$

(d) $\frac{1}{2} \ln |x - \sqrt{x^2 + 4}| + C$

(e) $\frac{x}{4\sqrt{x^2 + 4}} + C$

9. Evaluate $\int_0^\pi \sin^3(x) \cos^2(x) dx$.

(a) 2/15

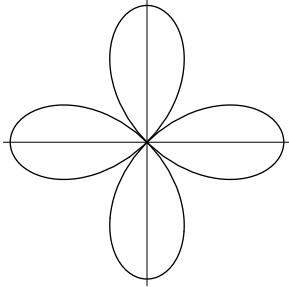
(b) 1/3

(c) 1/15

(d) 1/5

(e) 4/15

10. Compute the area inside one petal of the rose $r = \cos(2\theta)$.



(a) π

(b) $\pi/8$

(c) $\pi/2$

(d) $\pi/6$

(e) $\pi/4$

11. Find the limit $\lim_{x \rightarrow 0} (1+x)^{1/x}$

(a) ∞

(b) $1/e$

(c) e

(d) 1

(e) $e - 1$

12. Determine which is the best estimate for the error of approximating $\sum_{n=1}^{\infty} \frac{n}{e^{n^2}}$ using the partial sum s_4 .

(a) $\frac{4}{e^{16}}$

(b) $\frac{5}{e^{25}}$

(c) $\frac{1}{2e^{16}}$

(d) $\frac{1}{e^3(e-1)}$

(e) $\frac{1}{e^{15}(e-1)}$

13. Evaluate $\int \frac{1}{\sqrt{1-x^2}} dx$

(a) $\tan^{-1}(x) + C$

(b) $\sec^{-1}(x) + C$

(c) $\sqrt{1-x^2}/x + C$

(d) $\sqrt{1-x^2} + C$

(e) $\sin^{-1}(x) + C$

14. Find the equation of the line tangent to the curve $x = \frac{1}{t}$, $y = t^3$ at $t = \frac{1}{2}$.

(a) $y = \frac{3}{2}x + \frac{1}{8}$

(b) $y = -\frac{3}{16}x + \frac{1}{2}$

(c) $y = \frac{5}{8}x + \frac{1}{8}$

(d) $y = -x + \frac{1}{4}$

(e) $y = -\frac{1}{4}x + \frac{1}{2}$

15. Evaluate $\int_0^{10} 10^x dx$

(a) $(10^{11} - 1)/11$ (b) $10^{11}/11$ (c) $10^{10} - 1$

(d) $(10^{10} - 1)\ln(10)$ (e) $(10^{10} - 1)/\ln(10)$

16. Use power series to calculate $\lim_{x \rightarrow 0} \frac{x^6}{\cos(2x^3) - 1}$.

(a) $3/2$ (b) $-3/4$ (c) $-5/16$ (d) $-1/2$ (e) $1/16$

17. Evaluate $\int_0^1 x^2 e^x dx$

(a) $e - 1$ (b) $e/2$ (c) $e - 2$ (d) e (e) $e/2 - 1$

18. Find the interval of convergence of the power series $\sum_{n=1}^{\infty} \frac{(x-1)^{2n}}{4^n}$.

(a) $[0, 2]$ (b) $(-4, 4)$ (c) $(-1, 3)$ (d) $[0.5, 1.5]$ (e) $[0, 4)$

19. Solve the differential equation $y' = \tan(y)$.

(a) $y = \sin^{-1}(x + C)$ (b) $y = \sin^{-1}(Ce^x)$ (c) $y = \sin(x + C)$

(d) $y = Ce^{\sin(x)}$ (e) $y = Ce^{-\sin(x)}$

20. Evaluate $\int \frac{x-13}{x^2-2x-15} dx$

(a) $\ln \left| \frac{(x-5)^2}{x+3} \right| + C$ (b) $\ln |(x+3)^3(x-5)| + C$ (c) $\ln |(x-5)^3(x+3)| + C$

(d) $\frac{1}{2} \ln |x^2 - 2x - 15| + C$ (e) $\ln \left| \frac{(x+3)^2}{x-5} \right| + C$