Sociology 592 - Homework #9 - Intro to multiple regression, matrices

1. In the handout on 1-way ANOVA, we considered the following problem:

An economist wants to test whether mean housing prices are the same regardless of which of 3 air-pollution levels typically prevails. A random sample of house purchases in 3 areas yields the price data below.

Observation	Pollution Level					
	Low	Mod	High			
1	120	61	40			
2	68	59	55			
3	40	110	73			
4	95	75	45			
5	83	80	64			
Σ	406	385	277			

## MEAN HOUSING PRICES (THOUSANDS OF DOLLARS):

You will now consider an alternative approach to this problem. Let Y = Mean housing price. Let X1 = 1 if pollution is low, 0 if pollution is moderate, -1 if pollution is high. Let X2 = 0 if pollution is low, 1 if pollution is moderate, and -1 if pollution is high. The data for the <u>15</u> observations can then be written as follows:

X1	X2	Y	
1	0	120	
1	0	68	
1	0	40	
1	0	95	
1	0	83	
0	1	61	
0	1	59	
0	1	110	
0	1	75	
0	1	80	
-1	-1	40	
-1	-1	55	
-1	-1	73	
-1	-1	45	
-1	-1	64	

An old but still trustworthy version of SPSS produced the following:

\* \* \* \* MULTIPLE REGRESSION \* \* \* \* Listwise Deletion of Missing Data Mean Std Dev Variance Label 71.200 23.752 564.171 House Price Υ .000 .845 .714 Low Pollution .000 .845 .714 Moderate Pollution X1 X2 N of Cases = 15 Correlation, Covariance, 1-tailed Sig, Cross-Product: Y X1 X2 1.000 .459 .384 564.171 9.214 7.714 . .043 .079 7898.400 129.000 108.000 Y .459 1.000 .500 9.214 .714 .357 .043 . .029 129.000 10.000 5.000 X1 .384 .500 7.714 .357 .079 .029 108.000 5.000 1.000 Х2 .714 10.000 Equation Number 1 Dependent Variable.. Y House Price R Square (1) Standard Error (2) Analysis of Variance DF Sum of Squares Mean Square 2 (3) (4) Regression Residual 12 (5) (6) (7) F = Signif F = .1887----- Variables in the Equation -----В SE B Variable 95% Confdnce Intrvl B Beta T Siq T 

 x2
 (8)
 8.152709
 (9)
 23.563227
 .206376
 (10)
 .4904

 x1
 (11)
 (12)
 -7.763227
 (13)
 .355820
 1.227
 .2435

 (Constant)
 (14)
 5.764836
 58.639502
 83.760498
 (15)
 .0000

a) Fill in the missing entries (1) - (15). The information that has been left in, and possibly the results from our earlier discussion of this problem, can serve as double-checks on your answer.

b) What does this tell us about the relationship between level of pollution and housing prices?

c) Comment on how your results compare with our earlier analysis of this problem. What do you think the differences or similarities can be attributed to?

d) After you've done this by hand, you can double-check your answers using Hw09.sps – PROVIDED you can fix some syntax errors in the program and fill in the missing regression card.

2. An educator believes that the more hours per weekday a student's best friend spends on homework (ZHWORK), the more hours the student will tend to spend on homework (XHWORK). She also thinks that XHWORK will be affected by the student's socio-economic status (measured on a scale called XBBSESRW) and by whether or not the student is in the academic track (XTRKACAD - which is coded 1 if the student is in the academic track, 0 otherwise.) Using an old mainframe version of SPSS<sup>X</sup>, she obtains the following results:

	MEAN	STD DEV	LABEI	1					
XHWORK ZHWORK XTRKACAD XBBSESRW	3.975 .321	2.930 .467	TIME X IN	ON HO ACADE	OMEWORK EMIC TRA	PER ACK	WEEK		
CORRELATIO	)N:								
	XHW	ORK 2	ZHWORK	XTF	RKACAD	XBE	SESRW		
XHWORK ZHWORK XTRKACAD XBBSESRW	•		.326 1.000 .222 .152		.303 .222 1.000 .285		.179 .152 .285 1.000		
STANDARD E	ERROR	2.658	806						
ANALYSIS C		DF			SQUARES				
REGRESSION RESIDUAL		3 9299			0.80246 0.89382		4406 7		
F = 62	23.6993	5 5	SIGNIF	F =	.0000				
		VARIA	BLES IN						
VARIABLE		В		SE B	I	BETA		Т	SIG T
XBBSESRW ZHWORK XTRKACAD (CONSTANT)	1	.320998 .263356 .390122 .496854	.00	12126 9690 52694 19167	.264	1956	7.6 27.2 22.2 50.7	180 173	.0000
a)	С	ompute t	he fol	lowir	ng:				

- Compute the following:
  - The sample size 1.
  - R<sup>2</sup> (try calculating this at least 2 different ways and make sure your results 2. are consistent)
  - The 95% confidence interval for XTRKACAD 3.
  - 4. The covariance of XBBSESRW and XHWORK (i.e., SXBBSESRW, XHWORK)
  - 5. The cross-product of XBBSESRW and XTRKACAD (i.e. XP<sub>XBBSESRW,XTRKACAD</sub>, or, using our other notation, SP<sub>XBBSESRW,XTRKACAD</sub>
  - $M_{XTRKACAD, ZHWORK}$  (i.e.  $\Sigma$  (XTRKACAD \* ZHWORK)) 6.

b) Briefly discuss the implications of these findings. Answer such questions as, How much time per weekday does the average student spend on homework? What percentage of the students are in the academic track? Does it matter to students how much their friends study? If so, how much? Do students in the academic track tend to study more than students not in the academic track (once over variables are taken into account)? What is the most "important" determinant of how much a student studies? How much of the variation in time spent studying can these 3 variables account for, and how much variation must be due to other factors not yet considered?

c) To the best of your ability, discuss any theoretical or statistical problems you see with the above model specification. In particular, what problems might there be with using ZHWORK as an independent variable when XHWORK is the dependent variable? (I don't really expect you to get this, but see what you can come up with. This serves as a lead-in to a much broader discussion that occurs in later statistics classes.)

3. Construct ANOVA tables based on the following information. Also, report the value of  $R^2$  if it is not already given in the problem.

- a) Dependent variable: Occupational prestige Independent variables: Education, IQ, Father's occupational prestige  $n = 100, R^2 = .3, MSE = 10$
- b) Number of independent variables: 10. n = 50, F = 5, SSR = 80.
- c) Number of independent variables: 5.  $n = 100, R^2 = .4, s_y = 1.$

4. (Optional; this will be good extra practice if the calculations required in problem #2 are not enough for you to feel comfortable with the computational techniques.) Using the raw data presented in problem 1 (i.e. the data for X1, X2, and Y), compute the M, XP, s, and r matrices. (Once you have computed one quantity, you are free to use it when computing anything else, e.g. once you have the M matrix you don't have to keep on using the raw data.) Since SPSS reports everything except the M matrix, it ought to be pretty easy to double-check your answers.

5. Consider again the following problem (adapted from Hays, 4th edition, p. 607): In a study of the origins of gender stereotyping of young girls, a random sample of 35 intact families was taken, in which there was an oldest (or only) girl in the 9th grade. The father answered a questionnaire about his interest in sports and received a score X1. The mother answered a similar questionnaire and received a score X2. The physical education instructor of each girl rated her on general athletic ability, and this was used as variable X3. The dependent variable Y was the girl's own score on a questionnaire on interest in sports. We will use all the variables this time. Hw09.sps has everything you need, except you will have to add the regression command.

a. Regress Y on X1, X2, and X3.

b. Get the plot of Y on X1, X2, X3, and  $\hat{Y}$ . To do this, the last parameter on the regression card should be

 $/SCATTERPLOT\left(Y,X1\right)\left(Y,X2\right)\left(Y,X3\right)\left(Y,*PRED\right).$ 

- c. Which variable is most strongly correlated with Y? Who seems to have the stronger influence on the daughter, the father or the mother?
- d. What does  $R^2$  equal? What is the standard error of the estimate?
- e. If X1 = X2 = 30 and X3 = 10, what is the predicted value for Y?
- f. For each of the following, if  $\alpha = .05$ , should we reject or not reject the null hypothesis?

(i) $H_0: \beta_1 = 1$ (ii) $H_0: \beta_2 = 0$ (iii) $H_0: \beta_3 = 1$	
$H_A: \mathfrak{G}_1 \Leftrightarrow 1 \qquad \qquad H_A: \mathfrak{G}_2 \Leftrightarrow 0 \qquad \qquad H_A: \mathfrak{G}_3 \Leftrightarrow 1$	

6. Use Stata to confirm your answers to two or more of the following.

a. Problem 1a. You can use the file hw09-1.dta.

b. Problems 2a2 and 2a3. You can use the file hw09-2.dta. Or, you can create a pseudo-replication of the data, which is what I did. See the handout on using Stata for OLS regression. Your numbers will differ slightly because of rounding error.

c. Problem 4. You can do this even if you did not work the problem by hand. Again you can use hw09-1.dta. See the handout on using Stata with Multiple Regression & Matrices.

d. Problem 5a. You can use the file hw09-5.dta.