Sociology 592 - Homework #10 - Advanced Multiple Regression

1. In their classic 1982 paper, "Beyond Wives' Family Sociology: A Method for Analyzing Couple Data," Thomson and Williams examined the relationship between the subjective expected utility of children and childbearing expectations. Husbands and wives were presented with several possible consequences of having another child within the next 20 months. Products of their subjective probability of each consequence (0 = no chance...10 = certain) and their evaluation of the consequence (-3 = extremely bad...+3 = extremely good) were constructed to form "subjective expected utilities" of another child. For the analyses presented below, the subjective expected utilities "a fulfilled family life" (X1 for wives, X3 for husbands) and "watching another child grow and develop" (X2 for wives, X4 for husbands) were used as indicators of child utility. The dependent variable, Y, is wife's childbearing expectations. Wives and husbands were asked to estimate the likelihood that they would have another child within 20 months (1 = extremely unlikely...7 = extremely likely; only the wife's measure is presented here though). In the spss printout presented below, only the wife variables (X1, X2, and Y) are used in the regression analysis.

Mean Std Dev Label 11.360 11.450 W's SEU for fulfilled family life
22.340 10.890 W's SEU for watching another child grow X1 X2 3.640 2.660 W's Childbearing expectations Υ N of Cases = 340 Correlation: X1 X2 Y 1.000.470.628.4701.000.421.628.4211.000 X1 Х2 Υ Equation Number 1 Dependent Variable.. Y W's Childbearing expectations Multiple R.64398R Square.41471R Square ChangeAdjusted R Square.41124F ChangeStandard Error2.04104Signif F Change Analysis of Variance
 Analysis of variance
 DF
 Sum of Squares
 Mean Square

 Regression
 2
 994.73432
 497.36716

 Residual
 337
 1403.89408
 4.16586
 119.39130 Signif F = .0000 F = ----- Variables in the Equation -----Variable В SE B 95% Confdnce Intrvl B Beta SE Beta Correl Part Cor

 X1
 .128257
 .010969
 .106682
 .149833
 .552086
 .047214
 .628000
 .487308

 X2
 .039453
 .011533
 .016768
 .062138
 .161520
 .047214
 .421000
 .142568

 (Constant)
 1.301617
 .252942
 .804072
 1.799161

 1.799161 ----- Variables in the Equation ------Variable Partial Tolerance VIF T Sig T X1 .537238 .779100 1.284 11.693 .0000 X2 .183199 .779100 1.284 3.421 .0007 (Constant) 5.146 .0000

		Varia	bles not in th	ne Equati	on		
Variable	Beta In	Partial	Tolerance	VIF	Min Toler	Т	Sig T
X3 X4	.255428 .192958	.295754 .238633	.784685 .895172	1.274 1.117	.659420 .733926	5.675 4.504	.0000

a. According to the above analysis, which form of subjective expected utility is more important for determining childbearing expectations? Justify your answer by citing at least 2 or 3 pieces of evidence from the printout.

b. What is the squared semipartial for X1? How much would R^2 decline if X1 were dropped from the model?

c. If you were doing forward stepwise regression, what variable, if any, would be added next? Why?

2. The data is the same as above, except that the corresponding SEU measures for the husbands (X3 and X4) have been added to the model.

	Mean	Std Dev	Label						
X1 X2 X3 X4	11.360 22.340 9.750 18.500	11.450 10.890 10.730 10.300	W's SH W's SH H's SH H's SH	EU for fulfi EU for watch EU for fulfi	lled family ing another lled family	life child gro life child gro	W		
Y	3.640	2.660	W's Ch	nildbearing (expectations	511114 910			
N of Case	s = 340	1							
Correlati	on:								
	х	1	X2	Х3	X4	Y			
X1 X2 X3 x4	1.00 .47 .46 31	0 1	.000 .270 223	1.000	1 000				
Y	.62	8	.421	.498	.381	1.000			
Equation	Number 1	Depen	dent Va	ariable	Y W's Chil	dbearing	expectati	ons	
Multiple R Square Adjusted Standard	R R Square Error	.6895 .4754 .4692 1.9379	5 8 1 4						
Analysis	of Varian	ice	C11m	of Sauaraa	Moon Sau	270			
Regressio Residual	n	4 335	1	L140.49257 L258.13583	285.12 3.75	314 563			
F =	75.91887	Si	gnif F	= .0000					
				Variables in	the Equation				
Variable		В	SE B	95% Confdno	ce Intrvl B	Beta	SE Beta	Correl	Part Cor
X1 X2 X3 X4 (Constant)	.0332 .0292 .7123	(1) 271 .0 (5) 324 .0 303 .2	(2) 011002 (6) 011860 283045	.078521 (3) (7) .005995 .155533	.123175 (4) .074821 .052653 1.269074	.434102 .136212 .205330 .113546 (9)	.048857 .045042 .049050 .045923	.628000 .421000 .498000 (8)	.351579 .119661 .165643 .097836

	Vari	ables in the	Equation		
Variable	Partial	Tolerance	VIF	Т	Sig T
X1 X2 X3 X4 (Constant)	.436709 .163014 .222956 .133872	.655938 .771751 (10) .742424	1.525 1.296 1.537 (11)	8.885 3.024 4.186 2.473 2.517	.0000 .0027 .0000 .0139 .0123

a. Fill in the missing information (1) - (11). HINT: There are many ways to doublecheck your answers. Some approaches are far easier than others.

b. Do an F-test of the hypothesis H_0 : $\beta_3 = \beta_4 = 0$.

c. Do an F-test of the hypothesis H_0 : $\beta_1 = 0$.

d. Suppose the null hypothesis H_0 : $B_4 = 0$ is true. If we drew 10,000 samples, in how many of them would we expect to find a value of b_4 that is as big or bigger in magnitude as what we found here (i.e. how many samples would likely contain a value of b_4 that is bigger than .029324 or smaller than -.029324)?

e. Suppose we did two-tailed tests for each b coefficient separately (i.e., first we tested H₀: $\beta_1 = 0$, then we tested H₀: $\beta_2 = 0$, etc). If we are using the .01 level of significance, which coefficients will we conclude are statistically significant?

f. Suppose X2 was completely uncorrelated with the other three X variables, i.e. its tolerance equaled 1. What would the standard error of b_2 be? What would its semipartial correlation be?

g. Suppose the tolerance of X3 equaled 0. What would the standard error of b_3 be?

h. Using the standardized coefficients, confirm that the value of R^2 given in the printout is correct.

i. Suppose the following two variables were added to the model: X5 = 0 if black, 1 otherwise. X6 = 1 if black, 0 otherwise. Drawing on your knowledge of sociological and political theory and your mastery of statistics, do you think the effects of X5 and X6 would be statistically significant? Why or why not?

j. Interpret these results. Among other things, your discussion should mention the following:

1. Who tends to have a higher subjective expected utility of children - husbands or their wives?

2. Who tends to be more influential in determining childbearing expectations - the husband or the wife? What do you think is the simplest explanation for this finding?

3. Does the average wife think it is likely or unlikely that she will have another child in the next 20 months?

4. How strongly are childbearing expectations determined by the subjective expected utility of children?

k. Suppose you now did backwards stepwise regression using the .05 level of significance. What variable, if any, would be dropped from the model? Explain your answer. How would your answer change if you used the .01 level of significance?

3. In all of the following problems, Y = income (in thousands of dollars). Assume each sample only includes members of the groups mentioned, and that the sample size for each group is the same (e.g. there are 50 blacks and 50 whites; or, 100 Catholics, 100 Protestants, 100 Jews.)

a. X = 0 if black, 1 if white. If a = 10 and b = 5, what is the average white income? Average black income? Average income for the entire sample? (HINT: The average income for the entire sample is not \$10,000.)

b. X1 = 1 if Catholic, 0 if Protestant, -1 if Jewish. X2 = 0 if Catholic, 1 if Protestant, -1 if Jewish. a = 10, b1 = -1, b2 = -2.

Find the average income for each religious group and for the entire population.

c. The average male makes \$30,000, the average female \$20,000. X = 1 if male, 0 if female. Compute a and b.

- d. X1 = 1 if Sociologist, 0 if Political Scientist, -1 if Chemist.
 - X2 = 0 if Sociologist, 1 if Political Scientist, -1 if Chemist.

The average Sociologist makes 35,000 a year, the average Political Scientist makes 40,000, the average Chemist makes 60,000. Compute a, b₁, and b₂.

4. (This problem is adapted from <u>Education, Occupation, & Earnings</u>, by William H. Sewell and Robert M. Hauser. 1975, Academic Press. See especially pages 72 and 79.) Focusing on earnings as the end product of the achievement procedure, Sewell and Hauser did extensive research on the post-secondary schooling, occupational achievements, and earnings during the first 10 years after high school graduation of a large sample of young men who graduated from Wisconsin high schools in 1957. A portion of their analysis can be replicated using Hw10.sps. The variables examined are:

- V Father's educational attainment (i.e. years of education)
- M Mother's educational attainment
- X Status of father's occupation when son graduated from high school (Duncan SEI)
- I Parent's average income, 1957-1960 (in thousands of dollars)
- Q Son's score on Henmon-Nelson Test of Mental Ability
- U Son's educational attainment
- W Son's 1964 occupation (Duncan SEI)
- Y Canonically weighted average of son's 1965-1967 earnings (in thousands of

dollars)

[Note: The Duncan Socio-Economic Index is a measure of occupational prestige.]

In Hw10.sps, three models are estimated using these data:

- I. W is regressed on V and M
- II. W is regressed on X, Q, and U
- III. W is regressed on X, Q, U, V, and M.

Copy and run Hw10.sps. Use the printout to answer the following questions: [HINT: No calculations are required to answer any of these questions, the necessary numbers are in the printout]

a. On average, who is the best educated - the mother, the father, or the son? What does this suggest about educational mobility across generations?

b. According to Model I, should we accept or reject H_0 : $\beta_M = \beta_V = 0$? Use the .05 level of significance.

c. According to Model III, should we accept or reject H_0 : $\beta_M = \beta_V = 0$? Use the .05 level of significance.

d. Are your results from (b) and (c) consistent? If not, offer a possible sociological explanation for the discrepancy.

e. What would you say is the most important determinant of W, the son's 1964 occupational prestige? What is the second most important? Offer a brief sociological explanation as to why these two variables are more important than the rest.

NOTE: As an added bonus, Hw10.sps also contains the cards needed to double-check your answers to problem 2. You just need to un-comment the regression card. But of course, don't do this until AFTER you have worked the problems by hand.

5. Use Stata to replicate the results from problem 2. You can either use hw10-2.dta or create a pseudo-replication of the data using the corr2data command (which is what I did, since I do not have the original data). Specifically, use Stata to compute

- a. The means, correlations and standard deviations
- b. The metric coefficients and their 95% confidence intervals
- c. The standardized coefficients
- d. The tolerances and VIFs
- e. The semipartial and partial correlations

Note that each of the above will require the use of a different Stata command.