Post-Estimation Commands for MLogit

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These notes borrow heavily (sometimes verbatim) from Long & Freese, 2014 <u>Regression Models for Categorical</u> Dependent Variables Using Stata, 3rd Edition.

Many/most of the Stata & spost13 post-estimation commands work pretty much the same way for mlogit as they do for logit and/or ologit. We'll therefore concentrate primarily on the commands that are somewhat unique.

Making comparisons across categories. By default, mlogit sets the base category to the outcome with the most observations. You can change this with the basecategory option. mlogit reports coefficients for the effect of each independent variable on each category relative to the base category. Hence, you can easily see whether, say, yr89 significantly affects the likelihood of your being in the SD versus the SA category; but you can't easily tell whether yr89 significantly affects the likelihood of your being in, say, SD versus D, when neither is the base. You could just keep rerunning models with different base categories; but listcoef makes things easier by presenting estimates for all combinations of outcome categories.

. use https://www3.nd.edu/~rwilliam/statafiles/ordwarm2.dta
(77 & 89 General Social Survey)

,				- 1 /			
	mlogit	warm i.yr89	i.male	i.white ag	e ed	prst, b(4)	nolog

		egistic regres			Numbe LR ch Prob Pseud	2293 349.54 0.0000 0.0583	
	warm	Coef.	Std. Err.	Z	P> z	[95% Conf.	Interval]
SD	i						
	yr89		1010407	C 41	0 000	1 515040	0050457
	1989	-1.160197	.1810497	-6.41	0.000	-1.515048	8053457
	male						
	Men	1.226454	.167691	7.31	0.000	.8977855	1.555122
,	 white						
	white		.2641771	3.16	0.002	.3164484	1.352004
	age		.0052183		0.000	.0214487	.041904
	ed				0.000	209786	
	prst				0.552		
	_cons	7221679	.4928708	-1.4/	0.143	-1.688177	.2438411
D	i						
	yr89						
	1989	4255712	.1318065	-3.23	0.001	6839071	1672352
	male						
	Men	1.326716	.137554	9.65	0.000	1.057115	1.596317
_	 white						
	white hite		.1872718	2.20	0.028	.0455885	.7796804
		.0292275			0.000	.0208832	.0375718
	ed		.0283399		0.070	1068737	.0042167
	prst					023899	0021645
-	_cons	3088357	.3938354	-0.78	0.433	-1.080739	.4630676

A							
	yr89 1989	0625534	.1228908	-0.51	0.611	3034149	.1783082
	male Men	.8666833	.1310965	6.61	0.000	.6097389	1.123628
	white						
	White	.3002409	.1710551	1.76	0.079	0350211	.6355028
	age	.0066719	.0041053	1.63	0.104	0013744	.0147181
	ed	0330137	.0274376	-1.20	0.229	0867904	.020763
	prst	0017323	.0052199	-0.33	0.740	0119631	.0084985
	_cons	.3932277	.3740361	1.05	0.293	3398697	1.126325
SA		(base outco	ome)				

. listcoef 1.yr89, help

mlogit (N=2293): Factor change in the odds of warm

Variable: 1.yr89 (sd=0.490)

				b	Z	P> z	e^b	e^bStdX
			+					
SD	VS	D		-0.7346	-4.434	0.000	0.480	0.698
SD	vs	A		-1.0976	-6.705	0.000	0.334	0.584
SD	VS	SA	ĺ	-1.1602	-6.408	0.000	0.313	0.567
D	VS	SD		0.7346	4.434	0.000	2.085	1.433
D	VS	A		-0.3630	-3.395	0.001	0.696	0.837
D	VS	SA		-0.4256	-3.229	0.001	0.653	0.812
A	VS	SD		1.0976	6.705	0.000	2.997	1.712
A	VS	D		0.3630	3.395	0.001	1.438	1.195
A	VS	SA		-0.0626	-0.509	0.611	0.939	0.970
SA	VS	SD		1.1602	6.408	0.000	3.191	1.765
SA	VS	D		0.4256	3.229	0.001	1.530	1.232
SA	VS	A		0.0626	0.509	0.611	1.065	1.031
DDDAAAAAAAAAAAAAAAAAAA	VS VS VS VS VS VS VS VS VS	SA SD A SA SD D SA SD D D D	 	-1.1602 0.7346 -0.3630 -0.4256 1.0976 0.3630 -0.0626 1.1602 0.4256	-6.408 4.434 -3.395 -3.229 6.705 3.395 -0.509 6.408 3.229	0.000 0.000 0.001 0.001 0.000 0.001 0.611 0.000 0.001	0.313 2.085 0.696 0.653 2.997 1.438 0.939 3.191 1.530	0.56 1.43 0.83 0.81 1.71 1.19 0.97 1.76

```
b = raw coefficient
z = z-score for test of b=0
P>|z| = p-value for z-test
e^b = exp(b) = factor change in odds for unit increase in X
e^bStdX = exp(b*SD of X) = change in odds for SD increase in X
```

Based on the above, we see that yr89 has little effect on strongly agreeing versus agreeing. In every other contrast though, the difference is significant.

It is possible to get overwhelmed with output, at least if you do this for all variables. The pvalue option can limit the output to differences which are significant. Also, the positive option only shows the positive differences (if you flip the comparison the coefficient will go negative.)

. listcoef , help pvalue(.01) positive

mlogit (N=2293): Factor change in the odds of warm (P<0.01)

Variable: 1.yr89 (sd=0.490)

			b	Z	P> z	e^b	e^bStdX
D	vs SD	İ	0.7346	4.434	0.000	2.085	1.433
A	vs SD		1.0976	6.705	0.000	2.997	1.712
A	vs D	1	0.3630	3.395	0.001	1.438	1.195
SA	vs SD		1.1602	6.408	0.000	3.191	1.765
SA	vs D	1	0.4256	3.229	0.001	1.530	1.232

Variable: 1.male (sd=0.499)

		 +	b	Z	P> z	e^b	e^bStdX
D v	s SA s A s SA s SA	 	1.2265 0.4600 1.3267 0.8667	7.314 4.403 9.645 6.611	0.000 0.000 0.000 0.000	3.409 1.584 3.769 2.379	1.844 1.258 1.938 1.541

Variable: 1.white (sd=0.329)

		 	b		P> z	e^b	e^bStdX
SD	vs SA		0.8342	3.158	0.002	2.303	1.316

Variable: age (sd=16.779)

		 	b	Z	P> z	e^b	e^bStdX
SD SD D	vs A vs SA vs A	 	0.0250 0.0317 0.0226	5.578 6.070 6.789	0.000 0.000 0.000	1.025 1.032 1.023	1.521 1.701 1.460
D	vs SA		0.0292	6.865	0.000	1.030	1.633

Variable: ed (sd=3.161)

			b	Z	P> z	e^b	e^bStdX
D	vs SD		0.0923	3.374	0.001	1.097	1.339
A	vs SD	1	0.1106	3.945	0.000	1.117	1.418
SA	vs SD	1	0.1436	4.251	0.000	1.154	1.574

Variable: prst (sd=14.492)
b = raw coefficient

z = z-score for test of b=0

P>|z| = p-value for z-test

 $e^b = exp(b) = factor change in odds for unit increase in X <math>e^bStdX = exp(b^*SD of X) = change in odds for SD increase in X$

Using the .01 level of significance (which may be wise given the many comparisons that are being done) we see that white only clearly distinguished between those who strongly agree and those who strongly disagree. prst does not have any significant effects.

Using mlogtest for tests of the Multinomial Logistic Model.

The mlogtest command provides a convenient means for testing various hypotheses of interest. Incidentally, keep in mind that mlogit can also estimate a logistic regression model; ergo you might sometimes want to use mlogit instead of logit so you can take advantage of the mlogtest command.

Tests of independent variables. mlogtest can provide likelihood-ratio tests for each variable in the model. To do this yourself, you would have to estimate a series of models, store the results, and then use the lrtest command. mlogtest can automate this process.

. mlogtest, lr

LR tests for independent variables (N=2293)

Ho: All coefficients associated with given variable(s) are 0

		chi2	df	P>chi2
	-+-			
1.yr89		58.853	3	0.000
1.male		106.199	3	0.000
1.white		11.152	3	0.011
age		83.119	3	0.000
ed		21.087	3	0.000
prst		8.412	3	0.038

From the above, we can see that each variable's effects are significant at the .05 level.

If you happen to have a very large data set or a very complicated model, LR tests can take a long time. It may be sufficient to simply use Wald tests in such cases. Remember, a Wald test only requires the estimation of the constrained model. In Stata, we could just do this with a series of test commands. Again, mlogtest, using the wald parameter, can automate the process and also present results more succinctly:

. mlogtest, wald

Wald tests for independent variables (N=2293)

Ho: All coefficients associated with given variable(s) are 0

		chi2	df	P>chi2
	-+			
1.yr89		53.812	3	0.000
1.male		97.773	3	0.000
1.white		10.783	3	0.013
age		79.925	3	0.000
ed		20.903	3	0.000
prst		8.369	3	0.039
PISC	- 1	0.505	9	0.000

We see that both tests lead to very similar conclusions in this case. That is fairly common; it seems they are most likely to differ in borderline cases.

You can also use mlogtest to test sets of variables, e.g.

. mlogtest, lr set(1.white prst \ 1.white ed \ 1.yr89 1.male)

LR tests for independent variables (N=2293)

Ho: All coefficients associated with given variable(s) are 0

1	chi2	df	P>chi2
1.yr89 1.male 1.white age ed prst set_1 set_2	58.853 106.199 11.152 83.119 21.087 8.412 19.282 30.334	3 3 3 3 3 3 6 6	0.000 0.000 0.011 0.000 0.000 0.038 0.004 0.000
set_3	167.621	6	0.000
<pre>set_1 contains: set 2 contains:</pre>	_		

set 3 contains: 1.yr89 1.male

Tests for combining dependent categories. If none of the IVs significantly affects the odds of outcome m versus outcome n, we say that m and n are indistinguishable with respect to the variables in the model. If two outcomes are indistinguishable with respect to the variables in the model, you can obtain more efficient estimates by combining them. I often use this command to see if I can combine categories, even if, say, I am using a command like ologit. Again, you can use both Stata or spost13 commands, and you can do LR or Wald tests.

. mlogtest, lrcomb

LR tests for combining alternatives (N=2293)

Ho: All coefficients except intercepts associated with a given pair of alternatives are 0 (i.e., alternatives can be collapsed)

		chi2	df	P>chi2
SD & D	-+- 	43.864	6	0.000
SD & A		153.130	6	0.000
SD & SA		215.033	6	0.000
D & A		98.857	6	0.000
D & SA		191.730	6	0.000
A & SA		54.469	6	0.000

Based on the above, we see that no categories should be combined. Doing the same thing with Wald tests,

. mlogtest, combine

Wald tests for combining alternatives (N=2293)

Ho: All coefficients except intercepts associated with a given pair of alternatives are 0 (i.e., alternatives can be combined)

		chi2	df	P>chi2
	+-			
SD & D		41.018	6	0.000
SD & A		135.960	6	0.000
SD & SA		183.910	6	0.000
D & A		93.183	6	0.000
D & SA		167.439	6	0.000
A & SA		51.441	6	0.000

Independence of Irrelevant Alternatives (IIA) Tests. The Stata 12 Reference Manual (P. 710) explains the IIA assumption this way:

A stringent assumption of multinomial and conditional logit models is that outcome categories for the model have the property of independence of irrelevant alternatives (IIA). Stated simply, this assumption requires that the inclusion or exclusion of categories does not affect the relative risks associated with the regressors in the remaining categories. One classic example of a situation in which this assumption would be violated involves the choice of transportation mode; see McFadden (1974). For simplicity, postulate a transportation model with the four possible outcomes: rides a train to work, takes a bus to work, drives the Ford to work, and drives the Chevrolet to work. Clearly, "drives the Ford" is a closer substitute to "drives the Chevrolet" than it is to "rides a train" (at least for most people). This means that excluding "drives the Ford" from the model could be expected to affect the relative risks of the remaining options and that the model would not obey the IIA assumption.

The 3rd edition of Long & Freese (section 8.4, pp. 407-411) explains the assumption further, and also explains ways of testing it. Long & Freese include tests for IIA in their programs but do NOT encourage their use. They note that these tests often provide conflicting results (e.g. some tests reject the null while others do not) and that various simulation studies have shown that these tests are not useful for assessing violations of the IIA assumption. They further argue that the multinomial logit model works best when the alternatives are dissimilar and not just substitutes for one another (e.g. if your choices were take your car to work, take a blue bus, or take a red bus, the two bus alternatives would be very similar and the IIA assumption would likely be violated, whether the tests showed it or not).

Paul Allison has also raised concerns about the IIA tests; see his blog entry at http://www.statisticalhorizons.com/iia.

But, if some reviewer says you need to test the IIA assumption, here is how you can do it with mlogtest.

. mlogtest, iia

Hausman tests of IIA assumption (N=2293)

Ho: Odds(Outcome-J vs Outcome-K) are independent of other alternatives

		chi2	df	P>chi2
	-+-			
SD		-0.177	14	
D		-10.884	14	
А		-3.009	13	
SA		-1.606	14	

Note: A significant test is evidence against Ho.

Note: If chi2<0, the estimated model does not meet asymptotic assumptions.

suest-based Hausman tests of IIA assumption (N=2293)

Ho: Odds(Outcome-J vs Outcome-K) are independent of other alternatives

		chi2	df	P>chi2
	-+-			
SD		18.651	14	0.179
D		20.289	14	0.121
A		23.480	14	0.053
SA		11.381	14	0.656

Note: A significant test is evidence against Ho.

Small-Hsiao tests of IIA assumption (N=2293)

Ho: Odds (Outcome-J vs Outcome-K) are independent of other alternatives

	lnL(full)	lnL(omit)	chi2	df	P>chi2
- '	-1025.061 -718.007		13.226	14 14	0.509
'	-678.789	-673.072	11.433	14	0.652
SA	-936.474	-928.840	15.268	14	0.360

Note: A significant test is evidence against Ho.

In this example the tests say IIA has not been violated. Long & Freese give examples of where different tests reach different conclusions with the same set of data.

Measures of Fit. The fitstat command can be used the same as before, e.g.

- . quietly mlogit warm i.yr89 i.male i.white age ed prst, b(4) nolog
- . quietly fitstat, save
- . * Now drop prst, white & ed, the three least significant vars
- . quietly mlogit warm i.yr89 i.male age , b(4) nolog
- . fitstat, dif

	Current	Saved	Difference
Log-likelihood	 		
Model	-2848.592	-2820.998	-27.594
Intercept-only	-2995.770	-2995.770	0.000
Chi-square			
D (df=2281/2272/9)	5697.184	5641.996	55.188
LR $(df=9/18/-9)$	294.357	349.544	-55.188
p-value	0.000	0.000	0.000
R2			
McFadden	0.049	0.058	-0.009
McFadden (adjusted)	0.045	0.051	-0.006
Cox-Snell/ML	0.120	0.141	-0.021
Cragg-Uhler/Nagelkerke	0.130	0.153	-0.023
Count	0.412	0.424	-0.013
Count (adjusted)	0.061	0.081	-0.020
IC	 		
AIC	5721.184	5683.996	37.188
AIC divided by N	2.495	2.479	0.016
BIC (df=12/21/-9)	5790.035	5804.486	-14.451

Note: Likelihood-ratio test assumes current model nested in saved model.

Difference of 14.451 in BIC provides very strong support for current model.

Incidentally, note that the chi-square and AIC tests favor the full model; however, the BIC test prefers the model that drops the least significant variables, prst, white & ed. As we have seen before, the BIC test tends to lead to more parsimonious models, especially when the sample size is large.

Outliers. The leastlikely command can be used to identify the cases where the observed value was farthest from the predicted value. You might want to check such cases for coding errors or think if there are ways to modify the model so these cases are not so discrepant.

- . quietly mlogit $% \left(1\right) =\left(1\right) +\left(1\right) +\left$
- . leastlikely warm yr89 male white age ed prst

Outcome: 1 (SD)

+ -	Prob	 warm	yr89	male	white	age	ed	+ prst
112. 167. 212. 271. 286.	.0389264 .0355258 .0423206 .0352297 .0407416	SD SD SD SD SD	1989 1989 1989 1989	Women Women Women Women	White White White White NotWhite	46 37 50 20 54	16 15 16 12 12	57 61 62 31 34

Outcome: 2 (D)

	+								_
	Prob	warm	yr89	male	white	age	ed	prst	ļ
414.	1286143	D	1989	Women	White	19	12	50	
563.	.1175782	D	1989	Women	NotWhite	41	18	69	
675.	.1322747	D	1989	Women	White	25	16	50	
803.	.107113	D	1989	Women	NotWhite	30	16	60	
1001.	1288399	D	1989	Women	White	32	18	62	
	+								+

Outcome: 3 (A)

	i		warm	yr89	male	white	age	ed	prst
	١.								
1305.		.1621244	A	1977	Men	White	79	8	41
1344.		.1575535	A	1977	Men	White	72	7	22
1404.		.1625481	A	1977	Men	White	74	8	26
1449.		.1398363	A	1977	Men	White	71	4	23
1729.		.1303623	A	1977	Men	White	81	5	36
	- 1								1

Outcome: 4 (SA)

	+							+
	Prob	warm	-		white	_		-
1963.	.0313339	SA	1977	Men	White	64	6	26
2093.	.0372785	SA	1977	Men	White	48	4	17
2107.	.034017	SA	1977	Men	White	69	8	33
2119.	.0345335	SA	1977	Men	White	58	4	41
2138.	.0316978	SA	1977	Men	White	57	3	37
	+							+

Aids to Interpretation. These are much the same as we talked about before. Standardized coefficients, however, are a noteworthy exception:

```
. listcoef, std
option std not allowed after mlogit
```

This is because the y* rationale does not hold in a multinomial logit model, i.e. there is no underlying latent variable. (As we saw earlier, however, the listcoef command will still do X-standardization.)

Other commands, however, behave identically or almost identically to what we have seen before. For example, we can use the predict command to come up with predicted probabilities:

```
. quietly mlogit warm i.yr89 i.male i.white age ed prst, b(4) nolog
. predict SDlogit Dlogit Alogit SAlogit
(option pr assumed; predicted probabilities)
```

. list warm yr89 male white age ed prst SDlogit Dlogit Alogit SAlogit in 1/10, clean

	warm	yr89	male	white	age	ed	prst	SDlogit	Dlogit	Alogit	SAlogit
1.	SD	1977	Women	White	33	10	31	.14696	.2569168	.375222	.2209013
2.	SD	1977	Men	White	74	16	50	.1931719	.4962518	.2510405	.0595358
3.	SD	1989	Men	White	36	12	41	.074012	.3257731	.4686748	.1315401
4.	SD	1977	Women	White	73	9	36	.277139	.383207	.2358743	.1037797
5.	SD	1977	Women	White	59	11	62	.2066857	.2824558	.3317693	.1790893
6.	SD	1989	Men	White	33	4	17	.1461631	.383301	.3885765	.0819594
7.	SD	1977	Women	White	43	7	40	.2276894	.2719278	.3321202	.1682626
8.	SD	1977	Women	White	48	12	48	.1571982	.2740046	.358632	.2101651
9.	SD	1977	Men	White	27	17	69	.0970773	.259278	.477971	.1656736
10.	SD	1977	Men	White	46	12	50	.1997817	.3800453	.3360028	.0841702

The extremes (use findit extremes) command helps you to see who is most likely and least likely to be predicted to strongly disagree:

. extremes SDlogit warm yr89 male white age ed prst

12140078837										
2048.	obs:	SDlogit	warm	yr89	male	wh	ite	age	ed	prst
6124276913 D 1977 Men White 80 5 45 1714289597 SD 1977 Men White 67 3 32 2824378463 SD 1977 Men White 68 3 37 874426529 SD 1977 Men White 83 5 51	2048. 2241. 1855.	.011555 .0127511 .0131329	SA SA A	1989 1989 1989	Women Women Women	NotWh NotWh NotWh	nite nite nite	26 21 25	17 15 16	68 52 61 36 60
1714289597 SD 1977 Men White 67 3 32 2824378463 SD 1977 Men White 68 3 37 874426529 SD 1977 Men White 83 5 51										
2824378463 SD 1977 Men White 68 3 37 874426529 SD 1977 Men White 83 5 51			_		-			-		
	282.	.4378463	SD	1977	Men	White	68	3	37	
863479314 D 1977 Men White 54 0 40	87.	.4426529	SD D	1977		White White	83 54	0	51 40	

Based on the results, we see that fairly young white women in 1989 with high levels of education and occupational prestige were predicted to be the least likely to strongly disagree. Conversely, nonwhite elderly males in 1977 with low levels of education and generally low levels of occupational prestige had almost a 50% predicted probability of strongly disagreeing.

Other comments. See Long and Freese for detailed explanations of how different commands are working, e.g. they often show you how the same things could be done in Stata without their commands (albeit in a much more tedious process). They also offer detailed advice on graphing results.