

```
> with(LinearAlgebra);
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[&x, Add, Adjoint, BackwardSubstitute, BandMatrix, Basis, BezoutMatrix, BidiagonalForm, BilinearForm, CARE, CharacteristicMatrix, CharacteristicPolynomial, Column, ColumnDimension, ColumnOperation, ColumnSpace, CompanionMatrix, ConditionNumber, ConstantMatrix, ConstantVector, Copy, CreatePermutation, CrossProduct, DARE, DeleteColumn, DeleteRow, Determinant, Diagonal, DiagonalMatrix, Dimension, Dimensions, DotProduct, EigenConditionNumbers, Eigenvalues, Eigenvectors, Equal, ForwardSubstitute, FrobeniusForm, GaussianElimination, GenerateEquations, GenerateMatrix, Generic, GetResultDataType, GetResultShape, GivensRotationMatrix, GramSchmidt, HankelMatrix, HermiteForm, HermitianTranspose, HessenbergForm, HilbertMatrix, HouseholderMatrix, IdentityMatrix, IntersectionBasis, IsDefinite, IsOrthogonal, IsSimilar, IsUnitary, JordanBlockMatrix, JordanForm, KroneckerProduct, LA_Main, LUDecomposition, LeastSquares, LinearSolve, LyapunovSolve, Map, Map2, MatrixAdd, MatrixExponential, MatrixFunction, MatrixInverse, MatrixMatrixMultiply, MatrixNorm, MatrixPower, MatrixScalarMultiply, MatrixVectorMultiply, MinimalPolynomial, Minor, Modular, Multiply, NoUserValue, Norm, Normalize, NullSpace, OuterProductMatrix, Permanent, Pivot, PopovForm, QRDecomposition, RandomMatrix, RandomVector, Rank, RationalCanonicalForm, ReducedRowEchelonForm, Row, RowDimension, RowOperation, RowSpace, ScalarMatrix, ScalarMultiply, ScalarVector, SchurForm, SingularValues, SmithForm, StronglyConnectedBlocks, SubMatrix, SubVector, SumBasis, SylvesterMatrix, SylvesterSolve, ToeplitzMatrix, Trace, Transpose, TridiagonalForm, UnitVector, VandermondeMatrix, VectorAdd, VectorAngle, VectorMatrixMultiply, VectorNorm, VectorScalarMultiply, ZeroMatrix, ZeroVector, Zip]
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(1)

```
> v := Vector(3);
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$$v := \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

(2)

```
> v(1) := Pi;  
> v(2) := exp(1);  
> v(3) := 2;  
> v;
```

$$\begin{bmatrix} \pi \\ e \\ 2 \end{bmatrix}$$

(3)

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> f := x -> x^2 + 1;
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$$f := x \rightarrow x^2 + 1$$

(4)

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> w := Vector(f, 5);
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(5)

$$w := \begin{bmatrix} 2 \\ 5 \\ 10 \\ 17 \\ 26 \end{bmatrix} \quad (5)$$

> Norm(v);

$$\pi \quad (6)$$

> Norm(v, 2);

$$\sqrt{4 + \pi^2 + (e)^2} \quad (7)$$

> M := Matrix([[7,0,1,-3,5],
[2,-1,0,1,4],
[7,-3,2,-1,4],
[8,6,-2,-7,4],
[1,3,-5,7,5]]);

$$M := \begin{bmatrix} 7 & 0 & 1 & -3 & 5 \\ 2 & -1 & 0 & 1 & 4 \\ 7 & -3 & 2 & -1 & 4 \\ 8 & 6 & -2 & -7 & 4 \\ 1 & 3 & -5 & 7 & 5 \end{bmatrix} \quad (8)$$

> Transpose(M);

$$\begin{bmatrix} 7 & 2 & 7 & 8 & 1 \\ 0 & -1 & -3 & 6 & 3 \\ 1 & 0 & 2 & -2 & -5 \\ -3 & 1 & -1 & -7 & 7 \\ 5 & 4 & 4 & 4 & 5 \end{bmatrix} \quad (9)$$

> RowOperation(M, [2,1], -2/7);

$$\begin{bmatrix} 7 & 0 & 1 & -3 & 5 \\ 0 & -1 & -\frac{2}{7} & \frac{13}{7} & \frac{18}{7} \\ 7 & -3 & 2 & -1 & 4 \\ 8 & 6 & -2 & -7 & 4 \\ 1 & 3 & -5 & 7 & 5 \end{bmatrix} \quad (10)$$

> N:=Matrix(5);

N:=M;

for i from 2 to 5 do

N:=RowOperation(N, [i,1], -M(i,1)/7):

od:

$$N := \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$N := \begin{bmatrix} 7 & 0 & 1 & -3 & 5 \\ 2 & -1 & 0 & 1 & 4 \\ 7 & -3 & 2 & -1 & 4 \\ 8 & 6 & -2 & -7 & 4 \\ 1 & 3 & -5 & 7 & 5 \end{bmatrix} \quad (11)$$

`> M;`

$$\begin{bmatrix} 7 & 0 & 1 & -3 & 5 \\ 2 & -1 & 0 & 1 & 4 \\ 7 & -3 & 2 & -1 & 4 \\ 8 & 6 & -2 & -7 & 4 \\ 1 & 3 & -5 & 7 & 5 \end{bmatrix}$$

(12)

`> N;`

$$\begin{bmatrix} 7 & 0 & 1 & -3 & 5 \\ 0 & -1 & -\frac{2}{7} & \frac{13}{7} & \frac{18}{7} \\ 0 & -3 & 1 & 2 & -1 \\ 0 & 6 & -\frac{22}{7} & -\frac{25}{7} & -\frac{12}{7} \\ 0 & 3 & -\frac{36}{7} & \frac{52}{7} & \frac{30}{7} \end{bmatrix}$$

(13)

`> MatrixMatrixMultiply(M,N);`

$$\begin{bmatrix} 49 & -6 & -\frac{58}{7} & \frac{202}{7} & \frac{424}{7} \\ 14 & 19 & -\frac{150}{7} & \frac{128}{7} & \frac{160}{7} \\ 49 & 3 & -\frac{53}{7} & \frac{75}{7} & \frac{309}{7} \\ 56 & -30 & \frac{40}{7} & \frac{265}{7} & \frac{606}{7} \\ 7 & 69 & -\frac{368}{7} & \frac{33}{7} & \frac{190}{7} \end{bmatrix}$$

(14)

> M . N;

$$\begin{bmatrix} 49 & -6 & -\frac{58}{7} & \frac{202}{7} & \frac{424}{7} \\ 14 & 19 & -\frac{150}{7} & \frac{128}{7} & \frac{160}{7} \\ 49 & 3 & -\frac{53}{7} & \frac{75}{7} & \frac{309}{7} \\ 56 & -30 & \frac{40}{7} & \frac{265}{7} & \frac{606}{7} \\ 7 & 69 & -\frac{368}{7} & \frac{33}{7} & \frac{190}{7} \end{bmatrix}$$

(15)

> LinearSolve (M,w) ;

$$\begin{bmatrix} \frac{327}{136} \\ -\frac{1847}{136} \\ -\frac{367}{16} \\ -\frac{795}{136} \\ -\frac{513}{272} \end{bmatrix}$$

(16)

> M^5;

$$\begin{bmatrix} 31759 & 38688 & -35607 & 16285 & 50077 \\ 15290 & 22103 & -20636 & 10257 & 28040 \\ 30823 & 33093 & -32426 & 18711 & 51192 \\ 25448 & 35430 & -30450 & 9633 & 36324 \\ 10801 & 23691 & -26417 & 22351 & 38777 \end{bmatrix}$$

(17)