Lecture 2 Parallel Programming Platforms
Flynn’s Taxonomy

In 1966, Michael Flynn classified systems according to numbers of instruction streams and the number of data stream.

<table>
<thead>
<tr>
<th>Instruction Stream</th>
<th>Data Stream</th>
</tr>
</thead>
<tbody>
<tr>
<td>Single</td>
<td>Single</td>
</tr>
<tr>
<td>Multiple</td>
<td>Multiple</td>
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<table>
<thead>
<tr>
<th>SISD</th>
<th>SIMD</th>
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<tbody>
<tr>
<td>Single Uniprocessors</td>
<td>Processor arrays Pipelined vector processors</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>MISD</th>
<th>MIMD</th>
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<tbody>
<tr>
<td>Systolic arrays</td>
<td>Multiprocessors Multicomputers</td>
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</tbody>
</table>
SISD Machine

Example: single CPU computers (serial computer)

- Single instruction: Only one instruction stream is acted on by CPU during one clock cycle
- Single data: Only one data stream is used as input during one clock cycle
- Deterministic execution
SIMD Machine (I)

• A parallel computer
• It typically has a single CPU devoted exclusively to control, a large number of subordinate ALUs, each with its own memory and a high-bandwidth internal network.
• Control CPU broadcasts an instruction to all subordinate ALUs, and each of the subordinate ALUs either executes the instruction it is idle.
• Example: CM-1, CM-2, IBM9000
SIMD Machine (2)

Control CPU

ALU 0
Mem 0

ALU 1
Mem 1

ALU p
Mem p

Interconnection network
Figure 2.4  Executing a conditional statement on an SIMD computer with four processors: (a) the conditional statement; (b) the execution of the statement in two steps.
MIMD Machine (I)

- Most popular parallel computer architecture
- Each processor is a full-fledged CPU with both a control unit and an ALU. Thus each CPU is capable of executing its own program at its own space.
- Execution is *asynchronous*. Processors can also be specifically programmed to synchronize with each other.
- Examples: networked parallel computers, symmetric multiprocessor (SMP) computer.
MIMD Machine (II)

Further classification according to memory access:

- **Shared-memory** system
- **Distributed-memory** system (Message-passing)
Shared-Memory MIMD Machine (I)

- Multiple processors can operate independently, but share the same memory resources (a global address space).
- Change in a memory location made by one processor is visible to all other processors.
- Two classes of shared-memory architecture based on network connecting memory modules: Bus-based shared-memory architecture (SGI Challenge XL); Switch-Based architecture (Convex SPP1200).
- Classes of shared-memory systems based on time taken by a processor to access any memory: uniform memory access (UMA), NUMA.

Image recognition.
Image partitioned into 16 sections, each being analyzed by a different CPU. (Tanenbaum, Structured Computer Organization)
In principle, at a time, only one message is allowed to be sent. So poor performance.
Bus-based network

• A bus-based network consists of a shared medium that connects all nodes
• The cost of a bus-based network scales linearly with respect to the number of processors \( p \)
• The distance between any two nodes in the network is const. \( O(1) \).
• Ideal for broadcasting information
• Disadvantage: bounded bandwidth & blocking. Performance is not scalable with respect to the number of processors \( p \).
Shared-Memory MIMD Machine (III)

Switch-based shared-memory architecture, supports point-to-point communication among pairs of processing node and memory banks.

- Excellent performance
- Expensive
- Switch complexity is difficult to realize at high data rates
Crossbar network

• A crossbar network uses a grid of switches (or switching nodes) to connect $p$ processors to $b$ memory banks.

• It is non-blocking: connection of a processing node to a memory band does not block the connection of any other processing nodes to other memory banks.

• Usually, $b$ is at least on the order of $p$, the complexity of the crossbar network is $\Omega(p \times p)$.

• The total number of switches is $\Theta(pb)$

• Good performance scalability, bad cost scalability.
Shared-Memory MIMD Machine (IV)

• **Cache coherence**

For any shared-memory architecture that allows the caching of shared variables, if processor A updates a shared variable $x$ in its cache, how to make sure values of all copies of $x$ are current.

**Good News**: Cache coherence is achieved at the hardware level through **snoopy protocol** etc.
Distributed-Memory MIMD Machine (I)

- Each processor has its own private memory.
- A communication network is built to connect inter-processor memory.
- No concept of global address space of memory across all processors.
- No cache coherence concept.
- Data exchange is through message passing.

Image recognition. The image is split among the 16 memories. (Tanenbaum, Structured Computer Organization)
Case Study: LLNL Linux cluster architecture

From https://computing.llnl.gov/tutorials/linux_clusters/
Nodes

Front view of compute nodes from LC Opteron cluster

Quad-core, quad-socket Opteron compute node
Frames/Racks

An SU consists of: Nodes (compute, login, management, gateway)
First stage switches that connect to each node directly
Miscellaneous management hardware
Frames sufficient to house all of the hardware
Additionally, a second stage switch is also needed for every 2 SUs in a multi-SU cluster (not shown).
Interconnect overview

Two-stage interconnect, Atlas, Juno – 8SU

Adapter card: Processing node’s link to interconnect

First stage switch: Voltaire 24-port Switches and Nodes, Back

Second stage switch: Voltaire 288-port Switch, back. All used ports connect to first stage switches.
Interconnection Network (I)

- **Dynamic network switch**

  **Degree of the switch** = number of ports on a switch

  **Switch functions:**
  -- mapping from input to output ports
  -- internal buffering (when the requested output port is busy)
  -- routing (to reduce network congestion)
  -- multicasting (same output on multiple ports)
  -- non-blocking: disjoint paths between each pair of independent inputs and outputs
Switching Strategy

An interconnection network in the form of a four-switch square grid. **Circuit switching** is used. (Tanenbaum, Structured Computer Organization)

**Circuit switching**: before a packet is sent, the entire path from the source to the destination is reserved in advance.

**Store-and-forward packet switching**. (Tanenbaum, Structured Computer Organization)
Routing: the rule that determines which sequence of nodes a packet must follow from the source to the destination.

Deterministic routing: the scheme determines a unique path for a message. It does not use any information regarding the state of the network and may result in uneven use of the resources in a network.
- Example: dimension-ordered routing for mesh or hypercube.

Adaptive routing: the scheme uses the information regarding the current state of the network to determine the path of the message.
Network interface

• Network interface is to handle the connectivity between the node and the network
• It has input and output ports that pipe data from and to the network
• Function:
  --- packetizing data
  --- computing routing information
  --- buffering incoming and outgoing data
  --- error checking
Interconnection Network (II)

- **Static network (direct network):** point-to-point communication links between computing nodes
- **Dynamic network (indirect network):** built using switches and communication links. Communication links are connected to one another dynamically by switches to establish paths.
Interconnection Network (III)

• Linear array: each node has two neighbors

• 1D torus (ring)
Interconnection Network (IV)

- K-dimensional mesh: nodes have 2^k neighbors
Cray T3E

- Use Alpha 21164A processor with 4-way superscalar architecture, 2 floating point instruction per cycle
- CPU clock 675 MHz, with peak rating 1.35 Gigaflops, 512 MB local memory
- Parallel systems with 40 to 2176 processors (with modules of 8 CPUs each)
- **3D torus interconnect** with a single processor per node
- Each node contains a router and has a processor interface and six full-duplex link (one for each direction of the cube)
IBM BlueGene/L uses a three-dimensional (3D) torus network in which the nodes (red balls) are connected to their six nearest-neighbor nodes in a 3D mesh. In the torus configuration, the ends of the mesh loop back, thereby eliminating the problem of programming for a mesh with edges. Without these loops, the end nodes would not have six near neighbors.

In 1999, IBM Research announced a 5-year $100M project, named Blue Gene, to develop a petaflop computer for research in computational biology.
Interconnection Network (V)

**Hypercubes:** the topology has two nodes along each dimension and $\log_2 p$ dimensions.

- D-dimensional cube is constructed by connecting corresponding nodes of two (D-1) dimensional cube
- D-dimensional cube: P nodes in total, $D = \log_2 P$
- Distance between any two nodes is at most $\log P$. 
Binary Trees

Distance between any two nodes is no more than $2 \log p$

- Problem
  --- Messages from one half tree to another half tree are routed through the top level nodes
  — links closer to root carry more traffic than those at lower levels.
Interconnection Network (VII)

Fat Tree Network

- Increased the number of communication links and switching nodes closer to the root.
- The fat tree is suitable for dynamic networks

A fat tree network of 16 processing nodes
Interconnection Network (II)

- **Metrics for static network**

  **Diameter**: longest distance between two nodes – Indication of maximum delay that a message will encounter in being communicated between a pair of nodes.

  **Connectivity**: a measure of multiplicity of paths between any two nodes.

    Arc connectivity: minimum number of arcs that must be removed from the network to break it into two disconnected networks.

  **Bisection width**: minimum number of communication links that must be removed to partition the network into two equal halves – minimum volume of communication allowed between any two halves of the network.
## Metrics for static network topology

<table>
<thead>
<tr>
<th>Network</th>
<th>Diameter</th>
<th>Bisection Width</th>
<th>Arc Connect.</th>
<th>Number of Links</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fully conn-ted</td>
<td>1</td>
<td>$p^2 / 4$</td>
<td>$p-1$</td>
<td>$p(p-1)/2$</td>
</tr>
<tr>
<td>Star</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td>$p-1$</td>
</tr>
<tr>
<td>Binary tree</td>
<td>$2 \log((p+1)/2)$</td>
<td>1</td>
<td>1</td>
<td>$p-1$</td>
</tr>
<tr>
<td>Linear array</td>
<td>$p-1$</td>
<td>1</td>
<td>1</td>
<td>$p-1$</td>
</tr>
<tr>
<td>Ring</td>
<td>$</td>
<td>p-2</td>
<td>$</td>
<td>2</td>
</tr>
<tr>
<td>2D mesh</td>
<td>$2(\sqrt{p} - 1)$</td>
<td>$\sqrt{p}$</td>
<td>2</td>
<td>$2(p - \sqrt{p})$</td>
</tr>
<tr>
<td>2D meshwrap</td>
<td>$2\left\lfloor \sqrt{p/2} \right\rfloor$</td>
<td>$2\sqrt{p}$</td>
<td>4</td>
<td>$2p$</td>
</tr>
<tr>
<td>Hypercube</td>
<td>$\log p$</td>
<td>$p/2$</td>
<td>$\log p$</td>
<td>$p \log p / 2$</td>
</tr>
</tbody>
</table>
Cost Model for Communicating Messages

Time to communicate a message \( t_{comm} \) between two nodes in a network: sum of the time to prepare a message for transmission and the time taken by the message to traverse the network to its destination.

- **Startup time** \( t_s \): the time required to handle a message at sending and receiving nodes.
- **Pre-hop time** \( t_h \): the time taken by the header of a message to travel between two directly-connected nodes, which is also known as node latency. This time is directly related to the latency within the routing switch for determining which output buffer or channel the message should be forward to.
- **Per-word transfer time** \( t_w \): If the channel bandwidth is \( r \) words per second, then each word takes time \( t_w = 1/r \) to traverse the link.
$t_{comm}$ needs to send $m$ words to traverse $l$ communication link:

- **Store-and-forward switching:**
  When a message traverses a path with multiple links, each intermediate node on the path forwards the message to the next node after it has received and stored the entire message.

  $$t_{comm} = t_s + (t_h + t_w m)l$$

- **Cut-through switching:**
  A message is broken into fixed size units call flow control digits of flits. After the connection from source to destination is established, the flits are sent one after the other.

  $$t_{comm} = t_s + lt_h + t_w m$$
HPC configuration with HP BladeSystem solutions

Figure 7 shows a full-bandwidth, fat-tree configuration of HP BladeSystem c-Class components providing 576 nodes in a cluster. Each c7000 enclosure includes an HP 4x QDR InfiniBand Switch Blade, with 16 downlinks for server blade connection and 16 QSFP uplinks for fabric connectivity. Sixteen 36-port QDR InfiniBand switches provide spine-level fabric connectivity.

**Figure 7.** HP BladeSystem c-Class 576-node cluster configuration using BL280c blades

<table>
<thead>
<tr>
<th>Total nodes</th>
<th>576 (1 per blade)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Racks required for servers</td>
<td>Nine 42U</td>
</tr>
<tr>
<td></td>
<td>(assumes four c7000 enclosures per rack)</td>
</tr>
<tr>
<td>Interconnect</td>
<td>1:1 full bandwidth (non-blocking), 3 switch hops maximum, fabric redundancy</td>
</tr>
</tbody>
</table>
Nersc Carver

- Carver, a liquid-cooled IBM iDataPlex system, has 1202 compute nodes (9,984 processor cores). This represents a theoretical peak performance of 106.5 Teraflops/sec.

<table>
<thead>
<tr>
<th>Type of Node</th>
<th>Number</th>
<th>Cores/Node</th>
<th>Mem/Node</th>
<th>Mem/Core</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nehalem 2.67GHz &quot;smallmem&quot;</td>
<td>960</td>
<td>8</td>
<td>24GB 1333MHz</td>
<td>3 GB</td>
</tr>
<tr>
<td>Nehalem 2.67GHz &quot;bigmem&quot;</td>
<td>160</td>
<td>8</td>
<td>48GB 1066MHz</td>
<td>6 GB</td>
</tr>
<tr>
<td>Westmere 2.67GHz</td>
<td>80</td>
<td>12</td>
<td>48GB 1333MHz</td>
<td>4 GB</td>
</tr>
<tr>
<td>Nehalem-EX 2.00GHz</td>
<td>2</td>
<td>32</td>
<td>1TB 1066MHz</td>
<td>32 GB</td>
</tr>
</tbody>
</table>

**Interconnect**

All Carver nodes are interconnected by 4X QDR InfiniBand technology, meaning that 32 Gb/sec of point-to-point bandwidth is available for high-performance message passing and I/O. The interconnect consists of fiber optic cables arranged as local fat-trees within a global 2D mesh.
Additional Reference

- Using InfiniBand for a scalable compute infrastructure. Technology brief, 4th edition
- [https://computing.llnl.gov/tutorials/linux_clusters/](https://computing.llnl.gov/tutorials/linux_clusters/)
- [http://www.nersc.gov/](http://www.nersc.gov/)
- A.S. Tanenbaum, Structured Computer Organization