

```
> N:=5;  
i:=2;
```

$$\begin{aligned}N &:= 5 \\ i &:= 2\end{aligned}\tag{1}$$

```
> T:=1;
```

$$T := 1\tag{2}$$

```
> for j from 1 to N do  
if (j<>i) then T:= T*(x-a||j)  
fi;  
od;
```

```
> T;
```

$$(x - a1) (x - a3) (x - a4) (x - a5)\tag{3}$$

```
> with(LinearAlgebra):  
v:=Vector(N+1);  
for j from 0 to N do v[j+1]:=j/N; od:
```

$$v := \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}\tag{4}$$

```
> v;
```

$$\begin{bmatrix} 0 \\ \frac{1}{5} \\ \frac{2}{5} \\ \frac{3}{5} \\ \frac{4}{5} \\ 1 \end{bmatrix}\tag{5}$$

```
> L := proc( N::integer, i::integer, v::Vector, x)  
□ description "Lagrange function";  
local j,T;  
T:=1:  
for j from 0 to N do  
if (j<>i) then T:= T*(x-v[j+1])/(v[i+1]-v[j+1])  
fi;  
od;  
T;  
end proc;
```

```
L:=proc(N::integer, i::integer, v::Vector, x)
```

```
local j, T;  
description "Lagrange function";  
T:=1; for j from 0 to N do  
if j<>i then T:= T* (x - v[j + 1]) / (v[i + 1] - v[j + 1]) end if
```

(6)

```
end do;
```

```
T
```

```
end proc
```

```
> L(5,2,v,2);
```

- 1575

(7)

```
> int(L(5,2,v,x),x=0..1);
```

$\frac{25}{144}$

(8)

```
> for N from 1 to 4 do
print(N);
v:=Vector(N+1):
for j from 0 to N do v[j+1]:=j/N; od:
for i from 0 to N do
print(int(L(N,i,v,x),x=0..1)));
od: od:
```

1

$\frac{1}{2}$

$\frac{1}{2}$

2

$\frac{1}{6}$

$\frac{2}{3}$

$\frac{1}{6}$

3

$\frac{1}{8}$

$\frac{3}{8}$

$\frac{3}{8}$

$\frac{1}{8}$

4

$\frac{7}{90}$

$\frac{16}{45}$

$\frac{2}{15}$

$\frac{16}{45}$

$\frac{7}{90}$

(9)